Neutrosophic DEMATEL to Prioritize Risk Factors in Teenage Pregnancy

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Abstract: Care during pregnancy is a task of high importance for the health system. In Ecuador, special importance has been given to pregnant teenagers. However, there are various factors that influence pregnancy and in many cases it is not possible to prioritize their care. This research aims to develop a model to prioritize the factors that influence teenage pregnancy. The model operates using the neutrosophic DEMATEL method for the study of cause and effect in complex situations. The method implements as a principle the modeling of neutrality using neutrosophic numbers and allows evaluation through the use of linguistic terms, which is a natural form of evaluation for humans.

Keywords: DEMATEL; Neutrosophic Numbers; teenage pregnancy; risk factors.

1. Introduction

Starting to have sexual activity at an early age often leads to early pregnancies. Teenage pregnancy has been increasing in recent years [1]. Studies have registered that the maternal mortality rate in Ecuador continues to be high, approximately between 500 and 700 women die each year due to complications related to pregnancy [2]. Avoiding perinatal complications associated with teenage pregnancy constitutes a challenge for the Public Health system [3, 4]. Recent research has identified aspects related to teenage pregnancy that range from the psychological to the social [5, 6].

For the gestation process in adolescents, the influence of a set of critical factors determine the success of pregnancy [7]. Quantifying compliance with these factors would allow continuous evaluation and recommendation to the pregnant woman. Processes of this nature have been covered by science using Artificial Intelligence techniques to model uncertainty [8]. A critical factor is represented by a degree of compliance, a degree of neutrality, and a degree of uncertainty. In this context, the representation of the fulfillment of critical factors can be modeled using neutrosophic numbers [9].

This research aims to develop a model for the prioritization of risk factors in adolescent pregnancy. The model operates using the DEMATEL method that includes the calculation with neutrosophic sets [10-12]. Indeterminacy is part of daily life, which is why the neutrosophic DEMATEL allows the study of complex cause-effect relationships, which includes indeterminacy and the use of linguistic terms, which is the natural form of communication for human beings.

This article is structured in several sections. In the Materials and Methods section, we describe the structure of the proposed model from the implementation of a neutrosophic DEMATEL. Next, the Results section is developed; in which the proposed method is implemented in a case study, thereby demonstrating the applicability of the method proposed in the previous section. Finally the Conclusions and References are presented.

2. Preliminaries

This section describes the main definitions that make up the theoretical references on the object of study; such as the neutrosophic sets [13-15]. We also make a description of the Neutrosophic Single Value Sets [16] and the Neutrosophic Triangular Single Value Numbers [13, 17].
2.1 Definitions

Definition 1. Let X be a universe of discourse. A Neutrosophic Set (NS) is characterized by three membership functions, \( u_A(x), r_A(x), v_A(x) \) : \( X \rightarrow [0,1] \), which satisfy the condition \( 0 \leq u_A(x) + r_A(x) + v_A(x) \leq 3 \) for all \( x \in X \). \( u_A(x), r_A(x) \) and \( v_A(x) \) denote the membership functions to true, indeterminate and false of \( x \) in \( A \), respectively, and their images are standard or non-standard subsets of \( [0,1] \) (see [18],[19]).

Definition 2. Let \( X \) be a universe of discourse. A Single Value Neutrosophic Set (SVNS) \( A \) over \( X \) is an object of the form:

\[
A = \{(x, u_A(x), r_A(x), v_A(x)) : x \in X\}
\]

Where \( u_A, r_A, v_A : X \rightarrow [0,1] \), satisfy the condition \( 0 \leq u_A(x) + r_A(x) + v_A(x) \leq 3 \) for all \( x \in X \). \( u_A, r_A \) and \( v_A \) denote the membership functions of true, indeterminate and false of \( x \) in \( A \), respectively. For convenience, a Single Value Neutrosophic Number (SVNN) will be expressed as \( A = (a, b, c) \), where \( a, b, c \in [0,1] \) and satisfies \( 0 \leq a + b + c \leq 3 \) (see [18],[20]).

Definition 3. A Triangular Single Value Neutrosophic Number (TSVNN), which is denoted by: \( \tilde{a} = ((a_1, a_2, a_3); a_\beta, \beta_\alpha, \gamma_\alpha) \), is a CN over \( \mathbb{R} \), whose membership functions of truthfulness, indeterminacy, and falsehood are defined below (see [18],[21]):

\[
T_\alpha(x) = \begin{cases} 
\frac{a_1 x - a_2 a_1}{a_2 - a_1}, & x = a_2 \\
\frac{a_3 x - a_2 a_3}{a_3 - a_2}, & a_2 < x < a_3 \\
0, & \text{otherwise}
\end{cases}
\]

\[
I_\alpha(x) = \begin{cases} 
\frac{a_2 x - a_2 a_1 + \beta_\alpha (x - a_2)}{a_2 - a_1}, & a_1 = x < a_2 \\
\frac{(x - a_2 + \beta_\alpha (a_3 - x))}{a_3 - a_2}, & a_2 < x < a_3 \\
1, & \text{otherwise}
\end{cases}
\]

\[
F_\alpha(x) = \begin{cases} 
\frac{a_2 x - a_1}{a_2 - a_1}, & a_1 = x < a_2 \\
\frac{(x - a_2 + \gamma_\alpha (a_3 - x))}{a_3 - a_2}, & a_2 < x < a_3 \\
1, & \text{otherwise}
\end{cases}
\]

Where \( a_\beta, \beta_\alpha, \gamma_\alpha \in [0,1] \). \( a_1, a_2, a_3 \in \mathbb{R} \) and \( a_1 \leq a_2 \leq a_3 \).

Definition 4. Given \( \tilde{a} = ((a_1, a_2, a_3); a_\beta, \beta_\alpha, \gamma_\alpha) \) and \( \tilde{b} = ((b_1, b_2, b_3); a_\beta, \beta_\alpha, \gamma_\alpha) \) two TSVNN and \( \lambda \) is any non-zero real number. Then the following operations are defined:

Addition: \( \tilde{a} + \tilde{b} = ((a_1 + b_1, a_2 + b_2, a_3 + b_3); a_\beta \land \beta_\alpha \land \beta_\beta, \gamma_\alpha \land \gamma_\beta) \)

Subtraction: \( \tilde{a} - \tilde{b} = ((a_1 - b_1, a_2 - b_2, a_3 - b_3); a_\beta \land \beta_\alpha \land \beta_\beta, \gamma_\alpha \land \gamma_\beta) \)

Inversion: \( \tilde{a}^{-1} = ((a_3^{-1}, a_2^{-1}, a_1^{-1}); a_\beta, \beta_\alpha, \gamma_\alpha) \), donde \( a_1, a_2, a_3 \neq 0 \).

Product by a scalar:

\[
\lambda \tilde{a} = \begin{cases} 
((\lambda a_1, \lambda a_2, \lambda a_3); a_\beta, \beta_\alpha, \gamma_\alpha), & \lambda > 0 \\
((\lambda a_3, \lambda a_2, \lambda a_1); a_\beta, \beta_\alpha, \gamma_\alpha), & \lambda < 0
\end{cases}
\]
It is based on the DEMATEL Neutrosophic method, which will adapt to triangular and trapezoidal neutrosophic numbers.

Division of two TSVNN:
\[ \frac{a_1}{b_1} = \begin{cases} \left( \frac{a_1}{b_1}, a_2, a_3, b_2, b_3, b_1 \right); & a_3 > 0 \quad y_3 > 0 \\ \left( \frac{a_1}{b_1}, a_2, a_3, b_2, b_3, b_1 \right); & a_3 < 0 \quad y_3 < 0 \end{cases} \]

Multiplication of two TSVNN:
\[ \tilde{a} \tilde{b} = \begin{cases} \left( \frac{a_1}{b_1}, a_2, a_3, b_2, b_3, b_1 \right); & a_3 > 0 \quad y_3 > 0 \\ \left( \frac{a_1}{b_1}, a_2, a_3, b_2, b_3, b_1 \right); & a_3 < 0 \quad y_3 < 0 \end{cases} \]

Where, \( a \) is a t-norm and \( v \) is a t-conorm.

A t-norm is an operator \( T: [0,1]^2 \rightarrow [0,1] \) such that it satisfies the following axioms for all \( a, b, c \) and \( d \) in \( [0,1] \):
1. \( T(0,0) = 0, T(a,1) = a \) (Boundary conditions),
2. \( T(a,b) \leq T(c,d) \) if \( a \leq c \) and \( b \leq d \) (Monotony)
3. \( T(a,b) = T(b,a) \) (Commutativity)
4. \( T(a,T(b,c)) = T(T(a,b),c) \) (Associativity)

A t-conorm is an operator \( S: [0,1]^2 \rightarrow [0,1] \) such that it satisfies the following axioms for all \( a, b, c \) and \( d \) in \( [0,1] \):
1. \( S(1,1) = 1, S(a,0) = a \) (Boundary conditions),
2. \( S(a,b) \leq S(c,d) \) if \( a \leq c \) and \( b \leq d \) (Monotony)
3. \( S(a,b) = S(b,a) \) (Commutativity)
4. \( S(a,S(b,c)) = S(S(a,b),c) \) (Associativity)

To convert TSVNN into real numerical values, the following formulas are applied, known as Score Index and Precision Index, respectively:
\[
S(\tilde{a}) = \frac{1}{8} [a_1 + a_2 + a_3] (2 + a_3 - \beta_3 - \gamma_3) \quad (5)
\]
\[
A(\tilde{a}) = \frac{1}{8} [a_1 + a_2 + a_3] (2 + a_3 - \beta_3 + \gamma_3) \quad (6)
\]

3. Materials and Methods

The proposed model is structured in a workflow to prioritize the factors that influence teenage pregnancy. It is based on the DEMATEL Neutrosophic method, which will adapt to triangular and non-trapezoidal neutrosophic numbers [18]. Figure 1 shows a general diagram of the operation of the proposed model.

![Figure 1. Structure of the model](image-url)
Activity 1. Identify the objectives of the decision: compilation of the relevant information present in the problem. It consists of:

1. Selection of experts and decision-makers who have experience in the field under study. Let us denote the experts by E = {E₁, E₂,..., Eₚ} (k≥1).
2. Identify the relevant criteria that characterize the problem. They will be denoted by C = {C₁, C₂,...,Cₚ} (m≥2).

Activity 2. Establish comparison matrices: forming the comparison matrices by pairs of relevant criteria. The experts emit the k comparison matrices by pairs of criteria, with order m×m. For this, each expert must give a value to each criterion compared to another, in the form of TSVNN, evaluating according to the values shown in Table 1. The value of the element Xₗᵢ measures how much the factor Fₗ directly influences the factor Fᵢ, where Xₗᵢ = 0 if i = j. Table 1 shows the evaluation scales to measure the degree of influence between the factors.

<table>
<thead>
<tr>
<th>Linguistic Term</th>
<th>Corresponding Triangular Single Valued Neutrosophic Number</th>
</tr>
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<tbody>
<tr>
<td>No influence</td>
<td>0 = ((0, 0, 0); 0,50; 0,50; 0,50)</td>
</tr>
<tr>
<td>Low influence</td>
<td>1 = ((0, 1, 2); 0,30; 0,75; 0,70)</td>
</tr>
<tr>
<td>Medium influence</td>
<td>2 = ((1, 2, 3); 0,80; 0,15; 0,20)</td>
</tr>
<tr>
<td>High influence</td>
<td>3 = ((2, 3, 4); 0,90; 0,10; 0,10)</td>
</tr>
<tr>
<td>Very high influence</td>
<td>4 = ((4, 4, 4); 1,00; 0,00; 0,00)</td>
</tr>
</tbody>
</table>

Table 1. Linguistic terms that describe the relationship between two factors or criteria and their equivalent in TSVNN.

Activity 3. Calculate the matrix of direct relationships as the sum of the k comparison matrices and then divide by k, that is, the arithmetic mean of the previous matrices, where the operations between TSVNN of sum and product by the scalar 1/k. This matrix is called A = (Aₖ)ₘₙₚ.

Activity 4. Transformation of numerical values using the formula of Equations 5 or 6.

Activity 5. A is normalized by dividing it by s = max(max₁≤ₖ≤ₚ Σₗ=₁ₘ aₗᵢ, max₁≤ₖ≤ₚ Σₗ=₁ₘ aᵢₗ), it will be called Aₛ.

Activity 6. Calculate the total matrix of relationships using the following formula:

\[ T = Aₛ(1 − Aₛ)^{-1} \]  

(7)

Where I is the identity matrix of order m, the superscript -1 means inverse.

Activity 7. Calculate sum by rows and by columns of T = (Tₖ)ₘₙₚ. The sum by rows is denoted by D and the sum by columns is denoted by R. That is, D = [Σᵢ=₁ₘ Tᵢₗ]ₑₙₚ and R = [Σᵢ=₁ₘ Tₗᵢ]ₚₙ₁. Where the apostrophe indicates the matrix transposition.

Activity 8. Generation of relationship influence maps. For this, we calculate (R+D) called "Prominence" that measures the degree of central role that the factor or criterion plays within the system. While (R-D) is called "Ratio" and represents the effect that the factor or criterion produces in the system.

1. If rᵢ₋ⱼ > 0 the factor or criterion Cⱼ is located in the group of causes,
2. If rᵢ₋ⱼ < 0 the factor or criterion Cᵢ is located in the group of effects.

The pairs (R+D, R-D) can be represented graphically to give decision-makers a graphic idea about the system.

4. Results

This section presents the results of this research. It was carried out using data obtained from pregnant teenagers admitted at the Gynecology and Obstetrics service of Alfredo Noboa Montenegro Hospital in Guaranda, Ecuador. The study followed the sequence described in the model.

Three independent subject experts are selected, who issue their evaluations on the risk factors influencing adolescent pregnancy. The factors determined were those referred in [22] and that we reproduce below:

- F₁: Individual factors.
- F₂: Psychological factors.
- F₃: Family factors.
- F₄: Social factors.


Neutrosophic Sets and Systems, (Special Issue: Impact of Neutrosophy in solving the Latin American's social problems), Vol. 37, 2020
Tables 2, 3, 4 show the comparison matrices by pairs of criteria according to the evaluations issued by Experts 1, 2, 3 respectively. Table 5 contains the results of the aggregation using the arithmetic mean of the TSVNN shown in Tables 2, 3, 4. Min was used as t-norm and max as t-conorm.

All the calculations carried out in this article were made with Octave 4.2.1, which is a free software that uses the MATLAB language, and facilitates the operations with matrices, see [18].
From the matrix of total relations we have that

\[ D = [1.0000; 0.9375; 0.53125; 0.6875; 4.2500] \]
and

\[ R = [0.71875; 0.59375; 0.8750; 1.0625; 1] \],
see activity 7 of the model.

The vector \( R+D = [1.71875 \quad 1.53125 \quad 1.96875 \quad 1.59375 \quad 1.6875] \),
while \( R-D = [-0.28125 \quad -0.34375 \quad -0.21875 \quad 0.53125 \quad 0.3125] \). See also Figure 2, where the pairs \((R+D, R-D)\) are plotted.

![Graphical representation of the pairs (R + D, R-D). Each pair has a legend associated with the factor it represents.](image)

From Figure 2 we can notice that factors 4 and 5 are the main cause of the other factors.

**Conclusions**

This investigation implemented a model for prioritizing the factors that influence teenage pregnancy. The model based its inference process on the method known as DEMATEL neutrosophic for the study of cause and effect. The use of neutrosophic sets allowed the inclusion of uncertainty, indeterminacy and the use of linguistic terms. The evaluation of three experts was reviewed and the most important factors for the case under study were identified. As a result of the research, a case study was implemented based on data obtained from pregnant adolescents admitted at the Gynecology and Obstetrics service of the Alfredo Noboa Montenegro Hospital in Guaranda, Ecuador, from which it was possible to demonstrate the applicability of the presented proposal.

**References**


Received: April 20, 2020. Accepted: August 22, 2020