



## Information Fusion Using Plithogenic Set and Logic

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While the crisp, fuzzy, intuitionistic fuzzy, and neutrosophic sets are sets whose elements  $x$  are characterized by a single attribute, called "appurtenance", whose attribute values are: "membership" (for crisp sets and fuzzy sets), or "membership" and "nonmembership" (for intuitionistic fuzzy set), or "membership" and "nonmembership" and "indeterminacy" (for neutrosophic set), a plithogenic set is a set whose elements  $x$  are characterized by many attributes, and each attribute may have many attribute values [1-6].

Neutrosophic set was extended to plithogenic set by Smarandache in 2017.

### A simple example

Let's consider a set  $M = \{x_1, x_2, x_3\}$ , such that each element is characterized by two attributes:

$C = \text{color}$ ; and  $S = \text{size}$ . Suppose the attribute values of  $C = \{\text{white } (w), \text{blue } (b), \text{green } (g)\}$  and of size are  $S = \{\text{small } (s), \text{medium } (m)\}$ .

Thus, each  $x$  element of  $M$  is characterized by the all five attribute values: white, blue, green, small, tall, i.e.  $M = \{x_1(w, b, g; s, m), x_2(w, b, g; s, m), x_3(w, b, g; s, m)\}$ .

Therefore, each element  $x$  belongs to the set  $M$  with a degree of white  $d(w)$ , a degree of blue  $d(b)$ , a degree of green  $d(g)$ , a degree of small  $d(s)$ , and a degree of medium  $d(m)$ .

Thus,  $M = \{x_1(d_1(w), d_1(b), d_1(g); d_1(s), d_1(m)), x_2(d_2(w), d_2(b), d_2(g); d_2(s), d_2(m)), x_3(d_3(w), d_3(b), d_3(g); d_3(s), d_3(m))\}$

Where  $d_1(\cdot)$ ,  $d_2(\cdot)$ , and  $d_3(\cdot)$  are the degrees of appurtenance of  $x_1$ ,  $x_2$ , and  $x_3$  respectively to the set  $M$  with respect to each of the five attribute values.

But the degree of appurtenance may be: classical degree { whose values are 0 or 1 }, fuzzy degree { whose values are in  $[0, 1]$  }, intuitionistic fuzzy degree { whose values are in  $[0, 1]^2$  }, or neutrosophic degree { whose values are in  $[0, 1]^3$  }.

Therefore, we may get:

### A plithogenic classical set:

$M = \{x_1(0, 1, 0; 0, 1), x_2(1, 0, 0; 0, 0), x_3(1, 0, 0; 1, 0)\}$ , which means that:

$x_1$  is not white,  $x_1$  is blue,  $x_1$  is not green,  $x_1$  is not small,  $x_1$  is medium; similarly for  $x_2$  and  $x_3$ .

### A plithogenic fuzzy set:

$M = \{x_1(0.2, 0.7, 0.5; 0.8, 0.3), x_2(0.5, 0.1, 0.0; 0.9, 0.2), x_3(0.5, 1, 0.6; 0.4, 0.3)\}$ ,

which means that:

$x_1$  has the fuzzy degree of white equals to 0.2,  $x_1$  has the fuzzy degree of blue equals to 0.7,

$x_1$  has the fuzzy degree of green equals to 0.1,  $x_1$  has the fuzzy degree of small size equals to 0.8,

and  $x_1$  has the fuzzy degree of medium size equals to 0.3;

similarly for  $x_2$  and  $x_3$ .

### A plithogenic intuitionistic fuzzy set:

$M = \{x_1((0.4, 0.1), (0.2, 0.7), (0.0, 0.3); (0.8, 0.5), (0.2, 0.3)), x_2((0.7, 0.2), (0.2, 0.6), (1.0, 0.0); (0.6, 0.4), (0.1, 0.5)), x_3((0.4, 0.4), (0.5, 0.6), (0.5, 0.1); (0.5, 0.6), (0.3, 0.3))\}$ ;

which means that:

$x_1$  has the truth-degree of white equals to 0.4 and the false-degree of white equals to 0.1;

$x_1$  has the truth-degree of blue equals to 0.2 and the false-degree of blue equals to 0.7;

$x_1$  has the truth-degree of green equals to 0.0 and the false-degree of green equals to 0.3;

$x_1$  has the truth-degree of small size equals to 0.8 and the false-degree of small size equals to 0.5;

$x_1$  has the truth-degree of medium size equals to 0.2 and the false-degree of white equals to 0.3;

similarly for  $x_2$  and  $x_3$ .

**A plithogenic neutrosophic set:**

$M = \{ x_1( (0.2,0.4,0.3), (0.5,0.2,0.7), (0.6,0.4,0.3); (0.9,0.6,0.5), (0.1,0.2,0.3) ), x_2( (0.1,0.7,0.2), (0.3,0.2,0.7), (0.0,0.2,1.0); (0.6,0.6,0.1), (0.0,0.1,0.6) ), x_3( (0.7,0.4,0.4), (0.5,0.6, (0.3,0.5,0.1); (0.0,0.5,0.6), (0.8,0.3,0.2) );$

which means that:

$x_1$  has the truth-degree of white equals to 0.2, the indeterminacy-degree of white equals to 0.4, and the false-degree of white equals to 0.3;

$x_1$  has the truth-degree of blue equals to 0.5, the indeterminacy-degree of blue equals to 0.2, and the false-degree of blue equals to 0.7;

$x_1$  has the truth-degree of green equals to 0.6, the indeterminacy-degree of green equals to 0.4, and the false-degree of green equals to 0.3;

$x_1$  has the truth-degree of small size equals to 0.9, the indeterminacy-degree of small size equals to 0.6, and the false-degree of small size equals to 0.5;

$x_1$  has the truth-degree of medium size equals to 0.1, the indeterminacy-degree of minimum size equals to 0.2, and the false-degree of minimum size equals to 0.3;

similarly for  $x_2$  and  $x_3$ .

Of course, we have considered the Single-Valued Plithogenic Set, i.e. when all degrees are single-valued (crisp) numbers from  $[0, 1]$ .

But similarly we may define:

Interval-Valued Plithogenic Set (when the degrees are intervals included into  $[0, 1]$ ),

or Hesitant Plithogenic Set (when the degrees are discrete finite subsets included into  $[0, 1]$ ),

or in the most general case Subset Plithogenic Set (when the degrees are any subsets included into  $[0, 1]$ ).

**Using generic notations one has**

**Plithogenic fuzzy set**

$x(v_1(t_1), v_2(t_2), \dots, v_n(t_n))$

**Plithogenic intuitionistic fuzzy set**

$x(v_1(t_1, f_1), v_2(t_2, f_2), \dots, v_n(t_n, f_n))$ , with  $0 \leq t_j + f_j \leq 1$ , for all  $j \in \{1, 2, \dots, n\}$ .

**Plithogenic neutrosophic set**

$x(v_1(t_1, i_1, f_1), v_2(t_2, i_2, f_2), \dots, v_n(t_n, i_n, f_n))$ , with  $0 \leq t_j + i_j + f_j \leq 3$ , for all  $j \in \{1, 2, \dots, n\}$ .

where  $t_j, i_j, f_j \in [0, 1]$  are degrees of membership, indeterminacy, and nonmembership respectively. Plithogenic Set is much used in Multi-Criteria Decision Making.

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