

# Soft Neutrosophic Bi-LA-semigroup and Soft Neutrosophic N-LA-seigroup

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Abstract. Soft set theory is a general mathematical tool for dealing with uncertain, fuzzy, not clearly defined objects. In this paper we introduced soft neutrosophic bi-LA-semigroup, soft neutrosophic sub bi-LA-semigroup, soft neutrosophic N-LA-semigroup with the discuission of some of their characteristics. We also introduced a

new type of soft neutrophic bi-LAsemigroup, the so called soft strong neutrosophic bi-LAsemigoup which is of pure neutrosophic character. This is also extend to soft neutrosophic strong N-LA-semigroup. We also given some of their properties of this newly born soft structure related to the strong part of neutrosophic theory.

Keywords: Neutrosophic bi-LA-semigroup, Neutrosophic N-LA-semigroup, Soft set, Soft neutrosophic bi-LAisemigroup. Soft Neutrosophic N-LA-semigroup.

#### **1** Introduction

Florentine Smarandache for the first time introduced the concept of neutrosophy in 1995, which is basically a new branch of philosophy which actually studies the origin, nature, and scope of neutralities. The neutrosophic logic came into being by neutrosophy. In neutrosophic logic each proposition is approximated to have the percentage of truth in a subset T, the percentage of indeterminacy in a subset I, and the percentage of falsity in a subset F. Neutrosophic logic is an extension of fuzzy logic. In fact the neutrosophic set is the generalization of classical set, fuzzy conventional set, intuitionistic fuzzy set, and interval valued fuzzy set. Neutrosophic logic is used to overcome the problems of impreciseness, indeterminate, and inconsistencies of date etc. The theory of neutrosophy is so applicable to every field of algebra. W.B. Vasantha Kandasamy and Florentin Smarandache introduced neutrosophic fields, neutrosophic rings, neutrosophic vector spaces, neutrosophic groups, neutrosophic bigroups and neutrosophic N -groups, neutrosophic semigroups, neutrosophic bisemigroups, and neutrosophic N-semigroups, neutrosophic loops, nuetrosophic biloops, and neutrosophic N -loops, and so on. Mumtaz ali et. al. introduced nuetrosophic LA -semigroups . Soft neutrosophic LA-semigroup has been introduced by Florentin Smarandache et.al.

Molodtsov introduced the theory of soft set. This mathematical tool is free from parameterization inadequacy, syndrome of fuzzy set theory, rough set theory, probability theory and so on. This theory has been applied successfully in many fields such as smoothness of functions, game theory, operation research, Riemann integration, Perron integration, and probability. Recently soft set theory attained much attention of the researchers since its appearance and the work based on several operations of soft set introduced in [2,9,10]. Some properties and algebra may be found in [1]. Feng et al. introduced soft semirings in [5]. By means of level soft sets an adjustable approach to fuzzy soft set can be seen in [6]. Some other concepts together with fuzzy set and rough set were shown in [7,8].

In this paper we introduced soft nuetrosophic bi-LAsemigroup and soft neutrosophic N -LA-semigroup and the related strong or pure part of neutrosophy with the notions of soft set theory. In the proceeding section, we define soft neutrosophic bi-LA-semigroup, soft neutrosophic strong bi-LA-semigroup, and some of their properties are discussed. In the last section soft neutrosophic N -LAsemigroup and their corresponding strong theory have been constructed with some of their properties.

## **2** Fundamental Concepts

**Definition 1.** Let  $(BN(S), *, \circ)$  be a nonempty set with two binary operations \* and  $\circ$ .  $(BN(S), *, \circ)$  is said to be a neutrosophic bi-LA-semigroup if  $BN(S) = P_1 \cup P_2$ where atleast one of  $(P_1, *)$  or  $(P_2, \circ)$  is a neutrosophic LA-semigroup and other is just an LA- semigroup.  $P_1$  and  $P_2$  are proper subsets of BN(S).

If both  $(P_1, *)$  and  $(P_2, \circ)$  in the above definition are neutrosophic LA-semigroups then we call  $(BN(S), *, \circ)$ a strong neutrosophic bi-LA-semigroup.

**Definition 2.** Let  $(BN(S) = P_1 \cup P;:*,\circ)$  be a neutrosophic bi-LA-semigroup. A proper subset  $(T,\circ,*)$  is said to be a neutrosophic sub bi-LA-semigroup of BN(S) if

- 1.  $T = T_1 \cup T_2$  where  $T_1 = P_1 \cap T$  and  $T_2 = P_2 \cap T$  and
- At least one of (T<sub>1</sub>, ∘) or (T<sub>2</sub>, \*) is a neutrosophic LA-semigroup.

**Definition 3.** Let  $(BN(S) = P_1 \cup P, *, \circ)$  be a neutrosophic bi-LA-semigroup. A proper subset  $(T, \circ, *)$  is said to be a neutrosophic strong sub bi-LA-semigroup of

- BN(S) if
  - 1.  $T = T_1 \cup T_2$  where  $T_1 = P_1 \cap T$  and  $T_2 = P_2 \cap T$  and
  - 2.  $(T_1, \circ)$  and  $(T_2, *)$  are neutrosophic strong LAsemigroups.

**Definition 4.** Let  $(BN(S) = P_1 \cup P, *, \circ)$  be any neutrosophic bi-LA-semigroup. Let J be a proper subset of BN(S) such that  $J_1 = J \cap P_1$  and  $J_2 = J \cap P_2$  are ideals of  $P_1$  and  $P_2$  respectively. Then J is called the neutrosophic biideal of BN(S).

**Definition 5.** Let  $(BN(S), *, \circ)$  be a strong neutrosophic bi-LA-semigroup where  $BN(S) = P_1 \cup P_2$  with  $(P_1, *)$ and  $(P_2, \circ)$  be any two neutrosophic LA-semigroups. Let J be a proper subset of BN(S) where  $I = I_1 \cup I_2$  with  $I_1 = I \cap P_1$  and  $I_2 = I \cap P_2$  are neutrosophic ideals of the neutrosophic LA-semigroups  $P_1$  and  $P_2$  respectively. Then I is called or defined as the strong neutrosophic bildeal of BN(S).

**Definition 6.** Let  $\{S(N), *_1, ..., *_2\}$  be a non-empty set with N -binary operations defined on it. We call S(N) a neutrosophic N -LA-semigroup (N a positive integer) if the following conditions are satisfied.

- 1)  $S(N) = S_1 \cup ... S_N$  where each  $S_i$  is a proper subset of S(N) i.e.  $S_i \subset S_j$  or  $S_i \subset S_i$  if  $i \neq j$ .
- 2)  $(S_i, *_i)$  is either a neutrosophic LA-semigroup or an LA-semigroup for i = 1, 2, 3, ..., N.

If all the N -LA-semigroups  $(S_i, *_i)$  are neutrosophic LA-semigroups (i.e. for i = 1, 2, 3, ..., N) then we call S(N) to be a neutrosophic strong N -LA-semigroup.

# Definition 7. Let

 $S(N) = \{S_1 \cup S_2 \cup \dots S_N, *_1, *_2, \dots, *_N\}$  be a neutrosophic N -LA-semigroup. A proper subset  $P = \{P_1 \cup P_2 \cup \dots P_N, *_1, *_2, \dots, *_N\}$  of S(N) is said to be a neutrosophic sub N -LA-semigroup if  $P_i = P \cap S_i, i = 1, 2, \dots, N$  are sub LA-semigroups of  $S_i$  in which atleast some of the sub LA-semigroups are neutrosophic sub LA-semigroups.

# Definition 8. Let

 $S(N) = \{S_1 \cup S_2 \cup \dots S_N, *_1, *_2, \dots, *_N\} \text{ be a neutrosophic strong } N \text{ -LA-semigroup. A proper subset}$  $T = \{T_1 \cup T_2 \cup \dots \cup T_N, *_1, *_2, \dots, *_N\} \text{ of } S(N) \text{ is said to be a neutrosophic strong sub } N \text{ -LA-semigroup if } each (T_i, *_i) \text{ is a neutrosophic sub LA-semigroup of}$  $(S_i, *_i) \text{ for } i = 1, 2, \dots, N \text{ where } T_i = S_i \cap T.$ 

# Definition 9. Let

 $S(N) = \{S_1 \cup S_2 \cup \dots S_N, *_1, *_2, \dots, *_N\} \text{ be a neutro-sophic } N \text{ -LA-semigroup. A proper subset}$  $P = \{P_1 \cup P_2 \cup \dots \cup P_N, *_1, *_2, \dots, *_N\} \text{ of } S(N) \text{ is said to be a neutrosophic } N \text{ -ideal, if the following conditions are true,}$ 

1. P is a neutrosophic sub N -LA-semigroup of

2. Each  $P_i = S \cap P_i, i = 1, 2, ..., N$  is an ideal of  $S_i$ .

# **Definition 10.** Let

S(N).

 $S(N) = \{S_1 \cup S_2 \cup \dots S_N, *_1, *_2, \dots, *_N\} \text{ be a neutrosophic strong } N \text{-LA-semigroup. A proper subset} \\ J = \{J_1 \cup J_2 \cup \dots J_N, *_1, *_2, \dots, *_N\} \text{ where} \\ J_t = J \cap S_t \text{ for } t = 1, 2, \dots, N \text{ is said to be a neutrosophic strong } N \text{-ideal of } S(N) \text{ if the following conditions are satisfied.} \\ 1) \text{ Each it is a neutrosophic sub LA-semigroup of} \end{cases}$ 

 $S_t, t = 1, 2, ..., N$  i.e. It is a neutrosophic strong Nsub LA-semigroup of S(N).

2) Each it is a two sided ideal of  $S_t$  for t = 1, 2, ..., N. Similarly one can define neutrosophic strong N -left ideal or neutrosophic strong right ideal of S(N).

A neutrosophic strong N -ideal is one which is both a neutrosophic strong N -left ideal and N -right ideal of S(N).

#### Soft Sets

Throughout this subsection U refers to an initial universe, E is a set of parameters, P(U) is the power set of U, and  $A, B \subset E$ . Molodtsov defined the soft set in the following manner:

**Definition 11.** A pair (F, A) is called a soft set over Uwhere F is a mapping given by  $F: A \to P(U)$ . In other words, a soft set over U is a parameterized family of subsets of the universe U. For  $a \in A$ , F(a)may be considered as the set of a-elements of the soft set (F, A), or as the set of a-approximate elements of the soft set.

**Example 1.** Suppose that U is the set of shops. E is the set of parameters and each parameter is a word or sentence. Let

$$E = \begin{cases} \text{high rent, normal rent,} \\ \text{in good condition, in bad condition} \end{cases}$$

Let us consider a soft set (F, A) which describes the attractiveness of shops that Mr. Z is taking on rent. Suppose that there are five houses in the universe  $U=\{s_1,s_2,s_3,s_4,s_5\}\,$  under consideration, and that  $A=\{a_1,a_2,a_3\}\,$  be the set of parameters where

 $a_1$  stands for the parameter 'high rent,

 $a_{2}$  stands for the parameter 'normal rent,

 $a_{\rm 3}~$  stands for the parameter 'in good condition. Suppose that

$$\begin{split} F(a_1) &= \{s_1, s_4\} \text{ ,} \\ F(a_2) &= \{s_2, s_5\} \text{ ,} \\ F(a_3) &= \{s_3\}. \end{split}$$

The soft set (F, A) is an approximated family  $\{F(a_i), i = 1, 2, 3\}$  of subsets of the set U which gives us a collection of approximate description of an object. Then (F, A) is a soft set as a collection of approxima-

tions over U , where

$$\begin{split} F(a_1) &= high \ rent = \{s_1, s_2\}, \\ F(a_2) &= normal \ rent = \{s_2, s_5\}, \\ F(a_3) &= in \ good \ condition = \{s_3\}. \end{split}$$

**Definition 12.** For two soft sets (F, A) and (H, B) over U, (F, A) is called a soft subset of (H, B) if

1.  $A \subseteq B$  and

2.  $F(a) \subseteq H(a)$ , for all  $x \in A$ . This relationship is denoted by  $(F, A) \subset (H, B)$ . Similarly (F, A) is called a soft superset of (H, B) if (H, B) is a soft subset of (F, A) which is denoted by  $(F, A) \supset (H, B)$ .

**Definition 13.** Two soft sets (F, A) and (H, B) over U are called soft equal if (F, A) is a soft subset of (H, B) and (H, B) is a soft subset of (F, A).

**Definition 14.** Let (F, A) and (K, B) be two soft sets over a common universe U such that  $A \cap B \neq \phi$ . Then their restricted intersection is denoted by  $(F, A) \cap_R (K, B) = (H, C)$  where (H, C) is defined as  $H(c) = F(c) \cap K(c)$  for all  $c \in C = A \cap B$ .

**Definition 15.** The extended intersection of two soft sets (F, A) and (K, B) over a common universe U is the soft set (H, C), where  $C = A \cup B$ , and for all  $c \in C$ , H(c) is defined as

$$H(c) = \begin{cases} F(c) & \text{if } c \in A - B, \\ G(c) & \text{if } c \in B - A, \\ F(c) \cap G(c) & \text{if } c \in A \cap B. \end{cases}$$

We write  $(F, A) \cap_{\varepsilon} (K, B) = (H, C)$ .

**Definition 16.** The restricted union of two soft sets (F, A) and (K, B) over a common universe U is the soft set (H, C), where  $C = A \cup B$ , and for all  $c \in C$ , H(c) is defined as  $H(c) = F(c) \cup G(c)$  for all  $c \in C$ . We write it as  $(F, A) \cup_R (K, B) = (H, C)$ .

Definition 17. The extended union of two soft sets

 $(F,A) \mbox{ and } (K,B)$  over a common universe U is the soft set (H,C) , where  $\ C=A\cup B$  , and for all  $c\in C$  ,  $\ H(c)$  is defined as

$$H(c) = \begin{cases} F(c) & \text{if } c \in A - B \\ G(c) & \text{if } c \in B - A \\ F(c) \cup G(c) & \text{if } c \in A \cap B \end{cases}$$

We write  $(F, A) \cup_{\varepsilon} (K, B) = (H, C)$ .

# 3 Soft Neutrosophic Bi-LA-semigroup

**Definition 18.** Let BN(S) be a neutrosophic bi-LAsemigroup and (F, A) be a soft set over BN(S). Then (F, A) is called soft neutrosophic bi-LA-semigroup if and only if F(a) is a neutrosophic sub bi-LA-semigroup of BN(S) for all  $a \in A$ .

**Example 2.** Let  $BN(S) = \{ \langle S_1 \cup I \rangle \cup \langle S_2 \cup I \rangle \}$  be a

neutrosophic bi-LA-semigroup where

 $\langle S_1 \cup I \rangle = \{1, 2, 3, 4, 1I, 2I, 3I, 4I\}$  is a neutrosophic LA-semigroup with the following table.

-								
*	1	2	3	4	1I	21	31	4I
1	1	4	2	3	1I	4I	2I	3I
2	3	2	4	1	3I	2I	4I	1I
3	4	1	3	2	4I	1I	3I	2I
4	2	3	1	4	2I	3I	1I	4I
1I	1I	4I	2I	3I	1I	4I	2I	3I
2I	3I	2I	4I	1I	3I	2I	4I	1I
3I	4I	1I	3I	2I	4I	1I	3I	2I
4I	2I	3I	1I	4I	2I	3I	1I	4I

 $\langle S_2 \cup I \rangle = \{1, 2, 3, 1I, 2I, 3I\}$  be another neutrosophic bi-LA-semigroup with the following table.

*	1	2	3	1I	2I	3I
1	3	3	3	3I	3I	3I
2	3	3	3	3I	3I	3I
3	1	3	3	1I	3I	3I
1I	3I	3I	3I	3I	3I	3I
21	31	31	31	31	31	31
31	11	31	31	1I	31	31

Let  $A = \{a_1, a_2, a_3\}$  be a set of parameters. Then clearly

(F, A) is a soft neutrosophic bi-LA-semigroup over

BN(S), where

$$F(a_1) = \{1, 1I\} \cup \{2, 3, 3I\},$$
  

$$F(a_2) = \{2, 2I\} \cup \{1, 3, 1I, 3I\},$$
  

$$F(a_3) = \{4, 4I\} \cup \{1I, 3I\}.$$

**Proposition 1.** Let (F, A) and (K, D) be two soft neutrosophic bi-LA-semigroups over BN(S). Then

- 1. Their extended intersection  $(F, A) \cap_E (K, D)$ is soft neutrosophic bi-LA-semigroup over BN(S).
- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$ is soft neutrosophic bi-LA-semigroup over BN(S).
- 3. Their *AND* operation  $(F, A) \land (K, D)$  is soft neutrosophic bi-LA-semigroup over BN(S).

**Remark 1.** Let (F, A) and (K, D) be two soft neutrosophic bi-LA-semigroups over BN(S). Then

- 1. Their extended union  $(F, A) \cup_E (K, D)$  is not soft neutrosophic bi-LA-semigroup over BN(S).
- 2. Their restricted union  $(F, A) \cup_R (K, D)$  is not soft neutrosophic bi-LA-semigroup over BN(S).
- 3. Their *OR* operation  $(F, A) \lor (K, D)$  is not soft neutrosophic bi-LA-semigroup over BN(S).

One can easily proved (1), (2), and (3) by the help of examples.

**Definition 19.** Let (F, A) and (K, D) be two soft neutrosophic bi-LA-semigroups over BN(S). Then (K, D) is called soft neutrosophic sub bi-LA-semigroup of (F, A), if

- 1.  $D \subseteq A$ .
- 2. K(a) is a neutrosophic sub bi-LA-semigroup of F(a) for all  $a \in A$ .

**Example 3.** Let (F, A) be a soft neutrosophic bi-LAsemigroup over BN(S) in Example (1). Then clearly (K, D) is a soft neutrosophic sub bi-LA-semigroup of (F, A) over BN(S), where

$$K(a_1) = \{1, 1I\} \cup \{3, 3I\},$$
  
$$K(a_2) = \{2, 2I\} \cup \{1, 1I\}.$$

**Theorem 1.** Let (F, A) be a soft neutrosophic bi-LAsemigroup over BN(S) and  $\{(H_j, B_j): j \in J\}$  be a non-empty family of soft neutrosophic sub bi-LAsemigroups of (F, A). Then

- 1)  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic sub bi-LAsemigroup of (F, A).
- 2)  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic sub bi-LAsemigroup of (F, A).
- 3)  $\bigcup_{\substack{\mathcal{E}\\ j\in J}} (H_j, B_j)$  is a soft neutrosophic sub bi-LAsemigroup of (F, A) if  $B_j \cap B_k = \phi$  for all  $j, k \in J$ .

**Definition 20.** Let (F, A) be a soft set over a neutrosophic bi-LA-semigroup BN(S). Then (F, A) is called soft neutrosophic bideal over BN(S) if and only if F(a) is a neutrosophic bideal of BN(S), for all  $a \in A$ .

**Example 4.** Let  $BN(S) = \{\langle S_1 \cup I \rangle \cup \langle S_2 \cup I \rangle\}$  be a neutrosophic bi-LA-semigroup, where

 $\langle S_1 \cup I \rangle = \{1, 2, 3, 1I, 2I, 3I\}$  be another neutrosophic

bi-LA-semigroup with the following table.

*	1	2	3	1I	2I	3I
1	3	3	3	3I	3I	3I
2	3	3	3	3I	3I	3I
3	1	3	3	1I	3I	3I
1I	3I	3I	3I	3I	3I	3I
21	31	31	31	31	31	31
31	11	31	31	1I	31	31

P	And $S_2 \cup I / - \{1, 2, 3, 1, 2I, 5I\}$ be another neutro-									
S	sophic LA-semigroup with the following table.									
		1	2	3	Ι	21	3I			
	1	3	3	2	3I	3I	2I			
	2	2	2	2	2I	2I	2I			

2

2I

2I

2I

21

3I

2I

2I

2I

3I

2I

2I

21

2I

2I

2I

And  $\langle \mathbf{S} + \mathbf{I} \rangle = \langle \mathbf{I} \ \mathbf{2} \ \mathbf{Z} \ \mathbf{I} \ \mathbf{2I} \ \mathbf{I} \rangle$  he another neutro

Let  $A = \{a_1, a_2\}$  be a set of parameters. Then (F, A) is a soft neutrosophic bideal over BN(S), where

$$F(a_1) = \{1, 1I, 3, 3I\} \cup \{2, 2I\}, F(a_2) = \{1, 3, 1I, 3I\} \cup \{2, 3, 2I, 3I\}$$

**Proposition 2.** Every soft neutrosophic bildeal over a neutrosophic bi-LA-semigroup is trivially a soft neutrosophic bi-LA-semigroup but the conver is not true in general.

One can easily see the converse by the help of example.

**Proposition 3.** Let (F, A) and (K, D) be two soft neutrosophic biideals over BN(S). Then

- Their restricted union  $(F, A) \cup_{R} (K, D)$  is not a 1) soft neutrosophic biideal over BN(S).
- Their restricted intersection  $(F, A) \cap_R (K, D)$  is a 2) soft neutrosophic biideal over BN(S).
- Their extended union  $(F, A) \cup_{\varepsilon} (K, D)$  is not a 3) soft neutrosophic biideal over BN(S).
- Their extended intersection  $(F,A) \cap_{c} (K,D)$  is a 4) soft neutrosophic biideal over BN(S).

**Proposition 4.** Let (F, A) and (K, D) be two soft neutrosophic biideals over BN(S). Then

- Their OR operation  $(F, A) \lor (K, D)$  is not a 1. soft neutrosophic biideal over BN(S).
- 2. Their AND operation  $(F, A) \land (K, D)$  is a soft neutrosophic biideal over BN(S).

**Definition 21.** Let (F, A) and (K, D) be two soft neutrosophic bi-LA-semigroups over BN(S). Then

- (K, D) is called soft neutrosophic bideal of (F, A), if
- $B \subseteq A$ , and 1)
- K(a) is a neutrosophic bideal of F(a), for all 2)  $a \in A$ .

Example 5. Let (F, A) be a soft neutrosophic bi-LAsemigroup over BN(S) in Example (\*). Then (K,D) is a soft neutrosophic bildeal of (F,A) over BN(S), where

$$K(a_1) = \{1I, 3I\} \cup \{2, 2I\},\$$
  
$$K(a_2) = \{1, 3, 1I, 3I\} \cup \{2I, 3I\}.$$

Theorem 2. A soft neutrosophic biideal of a soft neutrosophic bi-LA-semigroup over a neutrosophic bi-LA\_semigroup is trivially a soft neutosophic sub bi-LAsemigroup but the converse is not true in general.

**Proposition 5.** If (F', A') and (G', B') are soft neutrosophic biideals of soft neutrosophic bi-LA-semigroups (F, A) and (G, B) over neutrosophic bi-LAsemigroups N(S) and N(T) respectively. Then  $(F', A') \times (G', B')$  is a soft neutrosophic bideal of soft neutrosophic bi-LA-semigroup  $(F, A) \times (G, B)$  over  $N(S) \times N(T)$ .

**Theorem 3.** Let (F, A) be a soft neutrosophic bi-LAsemigroup over BN(S) and  $\{(H_i, B_j): j \in J\}$  be a non-empty family of soft neutrosophic biideals of (F, A). Then

3

Ι

2I

3I

2

3I

2I

2I

2

3I

2I

2I

- 1)  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic ideal of (F, A).
- 2)  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic bideal of (F, A).
- 3)  $\bigcup_{j \in J} (H_j, B_j)$  is a soft neutrosophic bideal of (F, A).
- 4)  $\bigvee_{j \in J} (H_j, B_j)$  is a soft neutrosophic bideal of (F, A).

## 4 Soft Neutrosophic Storng Bi-LA-semigroup

**Definition 22.** Let BN(S) be a neutrosophic bi-LAsemigroup and (F, A) be a soft set over BN(S). Then (F, A) is called soft neutrosophic strong bi-LAsemigroup if and only if F(a) is a neutrosophic strong sub bi-LA-semigroup for all  $a \in A$ .

**Example 6.** Let BN(S) be a neutrosophic bi-LAsemigroup in Example (1). Let  $A = \{a_1, a_2\}$  be a set of parameters. Then (F, A) is a soft neutrosophic strong bi-LA-semigroup over BN(S), where

$$F(a_1) = \{1I, 2I, 3I, 4I\} \cup \{2I, 3I\},\$$

$$F(a_2) = \{1I, 2I, 3I, 4I\} \cup \{1I, 3I\}.$$

**Proposition 6.** Let (F, A) and (K, D) be two soft neutrosophic strong bi-LA-semigroups over BN(S). Then

- 1. Their extended intersection  $(F, A) \cap_E (K, D)$ is soft neutrosophic strong bi-LA-semigroup over BN(S).
- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$  is soft neutrosophic strong bi-LA-semigroup over BN(S).
- 3. Their *AND* operation  $(F, A) \land (K, D)$  is soft neutrosophic strong bi-LA-semigroup over

BN(S).

**Remark 2.** Let (F, A) and (K, D) be two soft neutrosophic strong bi-LA-semigroups over BN(S). Then

- 1. Their extended union  $(F, A) \cup_E (K, D)$  is not soft neutrosophic strong bi-LA-semigroup over BN(S).
- 2. Their restricted union  $(F, A) \cup_R (K, D)$  is not soft neutrosophic strong bi-LA-semigroup over BN(S).
- 3. Their *OR* operation  $(F, A) \lor (K, D)$  is not soft neutrosophic strong bi-LA-semigroup over BN(S).

One can easily proved (1), (2), and (3) by the help of examples.

**Definition 23.** Let (F, A) and (K, D) be two soft neutrosophic strong bi-LA-semigroups over BN(S). Then

(K, D) is called soft neutrosophic strong sub bi-LAsemigroup of (F, A), if

- 1.  $B \subseteq A$ .
- 2. K(a) is a neutrosophic strong sub bi-LAsemigroup of F(a) for all  $a \in A$ .

**Theorem 4.** Let (F, A) be a soft neutrosophic strong bi-LA-semigroup over BN(S) and  $\{(H_j, B_j): j \in J\}$ be a non-empty family of soft neutrosophic strong sub bi-LA-semigroups of (F, A). Then

- 1.  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong sub bi-LA-semigroup of (F, A).
- 2.  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong sub bi-LA-semigroup of (F, A).
- 3.  $\bigcup_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong

sub bi-LA-semigroup of (F, A) if  $B_i \cap B_k = \phi$  for all  $j, k \in J$ .

**Definition 24.** Let (F, A) be a soft set over a neutrosophic bi-LA-semigroup BN(S). Then (F, A) is called soft neutrosophic strong biideal over BN(S) if and only if F(a) is a neutrosophic strong biideal of BN(S), for all  $a \in A$ .

**Example 7.** Let BN(S) be a neutrosophic bi-LAsemigroup in Example (\*). Let  $A = \{a_1, a_2\}$  be a set of parameters. Then clearly (F, A) is a soft neutrosophic strong bildeal over BN(S), where

$$F(a_1) = \{1I, 3I\} \cup \{1I, 2I, 3I\},\$$
  
$$F(a_2) = \{1I, 3I\} \cup \{2I, 3I\}.$$

**Theorem 5.** Every soft neutrosophic strong bildeal over BN(S) is a soft neutrosophic bildeal but the converse is not true.

We can easily see the converse by the help of example.

**Proposition 7.** Every soft neutrosophic strong bildeal over a neutrosophic bi-LA-semigroup is trivially a soft neutrosophic strong bi-LA-semigroup but the converse is not true in general.

**Proposition 8.** Every soft neutrosophic strong bildeal over a neutrosophic bi-LA-semigroup is trivially a soft neutrosophic bi-LA-semigroup but the converse is not true in general.

One can easily see the converse by the help of example.

**Proposition 9.** Let (F, A) and (K, D) be two soft neutrosophic strong bildeals over BN(S). Then

- 1. Their restricted union  $(F, A) \cup_R (K, D)$  is not a soft neutrosophic strong bildeal over BN(S).
- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$ is a soft neutrosophic strong bildeal over BN(S).
- 3. Their extended union  $(F, A) \cup_{\varepsilon} (K, D)$  is not

a soft neutrosophic strong bildeal over BN(S).

- 4. Their extended intersection  $(F, A) \cap_{\varepsilon} (K, D)$ is a soft neutrosophic strong biideal over BN(S).
- 5. Their *OR* operation  $(F, A) \lor (K, D)$  is not a soft neutrosophic biideal over BN(S).
- 6. Their AND operation  $(F, A) \land (K, D)$  is a soft neutrosophic bildeal over BN(S).

**Definition 25.** Let (F, A) and (K, D) be two soft neutrosophic strong bi- LA-semigroups over BN(S). Then (K, D) is called soft neutrosophic strong biideal of (F, A), if

- 1.  $D \subseteq A$ , and
- 2. K(a) is a neutrosophic strong bildeal of F(a), for all  $a \in A$ .

**Theorem 6.** A soft neutrosophic strong biideal of a soft neutrosophic strong bi-LA-semigroup over a neutrosophic bi-LA\_semigroup is trivially a soft neutosophic strong sub bi-LA-semigroup but the converse is not true in general.

**Proposition 10.** If (F', A') and (G', B') are soft neutrosophic strong bideals of soft neutrosophic bi-LA-semigroups (F, A) and (G, B) over neutrosophic bi-LA-semigroups N(S) and N(T) respectively. Then  $(F', A') \times (G', B')$  is a soft neutrosophic strong bideal of soft neutrosophic bi-LA-semigroup  $(F, A) \times (G, B)$  over  $N(S) \times N(T)$ .

**Theorem 7.** Let (F, A) be a soft neutrosophic strong bi-LA-semigroup over BN(S) and  $\{(H_j, B_j): j \in J\}$ be a non-empty family of soft neutrosophic strong bideals of (F, A). Then

1. 
$$\bigcap_{j \in J} (H_j, B_j)$$
 is a soft neutrosophic strong bi

Mumtaz Ali, Florentin Smarandache and Muhammad Shabir, Soft Neutrosophic Bi-LA-semigroup and Soft Neutrosophic N-LA-seigroup

ideal of (F, A).

- 2.  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong biideal of (F, A).
- 3.  $\bigcup_{\substack{\mathcal{E}\\ j\in J}} (H_j, B_j)$  is a soft neutrosophic strong bideal of (F, A).
- 4.  $\bigvee_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong bideal of (F, A).

#### 5 Soft Neutrosophic N-LA-semigroup

**Definition 26.** Let  $\{S(N), *_1, *_2, ..., *_N\}$  be a

neutrosophic N-LA-semigroup and (F, A) be a soft set over S(N).

Then (F, A) is called soft neutrosophic N-LA-semigroup

if and only if F(a) is a neutrosophic sub N-LA-

semigroup of S(N) for all  $a \in A$ .

**Example 8.** Let  $S(N) = \{S_1 \cup S_2 \cup S_3, *_1, *_2, *_3\}$  be a

neutrosophic 3-LA-semigroup where

$$S_1 = \{1, 2, 3, 4, 1I, 2I, 3I, 4I\}$$
 is a neutrosophic LA-

semigroup with the following table.

*	1	2	3	4	1I	21	31	4I
1	1	4	2	3	1I	4I	2I	3I
2	3	2	4	1	3I	2I	4I	1I
3	4	1	3	2	4I	1I	3I	2I
4	2	3	1	4	2I	3I	1I	4I
1I	1I	4I	2I	3I	1I	4I	2I	3I
2I	3I	2I	4I	1I	3I	2I	4I	1I
3I	4I	1I	3I	2I	4I	1I	3I	2I
4I	2I	3I	1I	4I	2I	3I	1I	4I

 $S_2 = \{1, 2, 3, 1I, 2I, 3I\}$  be another neutrosophic bi-LAsemigroup with the following table.

*	1	2	3	1I	21	31
1	3	3	3	3I	3I	3I
2	3	3	3	3I	3I	3I
3	1	3	3	1I	3I	3I
1I	3I	3I	3I	3I	3I	3I
21	31	31	31	31	31	31
3I	1I	3I	31	1I	3I	3I

And  $S_3 = \{1, 2, 3, I, 2I, 3I\}$  is another neutrosophic LA-

semigroup with the following table.

	1	2	3	Ι	2I	3I
1	3	3	2	31	31	21
2	2	2	2	2I	21	2I
3	2	2	2	2I	21	2I
Ι	3I	3I	2I	3I	3I	2I
21	21	21	21	21	21	21
31	21	21	21	21	21	21

Let  $A = \{a_1, a_2, a_3\}$  be a set of parameters. Then clearly

(F, A) is a soft neutrosophic 3-LA-semigroup over

S(N), where

$$F(a_1) = \{1, 1I\} \cup \{2, 3, 3I\} \cup \{2, 2I\},\$$

$$F(a_2) = \{2, 2I\} \cup \{1, 3, 1I, 3I\} \cup \{2, 3, 2I, 3I\},\$$

$$F(a_3) = \{4, 4I\} \cup \{1I, 3I\} \cup \{2I, 3I\}.$$

**Proposition 11.** Let (F, A) and (K, D) be two soft neutrosophic N-LA-semigroups over S(N). Then

- 1. Their extended intersection  $(F, A) \cap_E (K, D)$ is soft neutrosophic N-LA-semigroup over S(N).
- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$ is soft neutrosophic N-LA-semigroup over S(N).
- 3. Their *AND* operation  $(F, A) \land (K, D)$  is soft neutrosophic N-LA-semigroup over S(N).

**Remark 3.** Let (F, A) and (K, D) be two soft neutrosophic N-LA-semigroups over S(N). Then

- 1. Their extended union  $(F, A) \cup_E (K, D)$  is not soft neutrosophic N-LA-semigroup over S(N).
- 2. Their restricted union  $(F, A) \cup_R (K, D)$  is not soft neutrosophic N-LA-semigroup over S(N).
- 3. Their *OR* operation  $(F, A) \lor (K, D)$  is not soft neutrosophic N-LA-semigroup over S(N).

One can easily proved (1), (2), and (3) by the help of examples.

**Definition 27.** Let (F, A) and (K, D) be two soft neutrosophic N-LA-semigroups over S(N). Then (K, D) is called soft neutrosophic sub N-LA-semigroup of (F, A), if

- 1.  $D \subseteq A$ .
- 2. K(a) is a neutrosophic sub N-LA-semigroup of F(a) for all  $a \in A$ .

**Theorem 8.** Let (F, A) be a soft neutrosophic N-LAsemigroup over S(N) and  $\{(H_j, B_j): j \in J\}$  be a non-empty family of soft neutrosophic sub N-LAsemigroups of (F, A). Then

1.  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic sub N-LA-semigroup of (F, A).

- 2.  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic sub N-LA-semigroup of (F, A).
- 3.  $\bigcup_{j \in J} (H_j, B_j)$  is a soft neutrosophic sub N-LA-semigroup of (F, A) if  $B_j \cap B_k = \phi$  for all  $j, k \in J$ .

**Definition 28.** Let (F, A) be a soft set over a neutrosophic N-LA-semigroup S(N). Then (F, A) is called soft neutrosophic N-ideal over S(N) if and only if F(a) is a neutrosophic N-ideal of S(N) for all  $a \in A$ .

**Example 9.** Consider Example (\*\*\*).Let  $A = \{a_1, a_2\}$  be a set of parameters. Then (F, A) is a soft neutrosophic 3ideal over S(N), where

$$F(a_1) = \{1, 1I\} \cup \{3, 3I\} \cup \{2, 2I\},\$$

$$F(a_2) = \{2, 2I\} \cup \{1I, 3I\} \cup \{2, 3, 3I\}.$$

**Proposition 12.** Every soft neutrosophic N-ideal over a neutrosophic N-LA-semigroup is trivially a soft neutrosophic N-LA-semigroup but the converse is not true in general.

One can easily see the converse by the help of example.

**Proposition 13.** Let (F, A) and (K, D) be two soft neutrosophic N-ideals over S(N). Then

- 1. Their restricted union  $(F, A) \cup_R (K, D)$  is not a soft neutrosophic N-ideal over S(N).
- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$ is a soft neutrosophic N-ideal over S(N).
- 3. Their extended union  $(F, A) \cup_{\varepsilon} (K, D)$  is not a soft neutrosophic N-ideal over S(N).

4. Their extended intersection  $(F, A) \cap_{\varepsilon} (K, D)$ is a soft neutrosophic N-ideal over S(N).

**Proposition 15.** Let (F, A) and (K, D) be two soft neutrosophic N-ideals over S(N). Then

- 1. Their *OR* operation  $(F, A) \lor (K, D)$  is a not soft neutrosophic N-ideal over S(N).
- 2. Their AND operation  $(F, A) \land (K, D)$  is a soft neutrosophic N-ideal over S(N).

**Definition 29.** Let (F, A) and (K, D) be two soft neutrosophic N-LA-semigroups over S(N). Then (K, D) is called soft neutrosophic N-ideal of (F, A), if

- 1.  $B \subseteq A$ , and
- 2. K(a) is a neutrosophic N-ideal of F(a) for all  $a \in A$ .

**Theorem 8.** A soft neutrosophic N-ideal of a soft neutrosophic N-LA-semigroup over a neutrosophic N-LAsemigroup is trivially a soft neutosophic sub N-LAsemigroup but the converse is not true in general.

**Proposition 16.** If (F', A') and (G', B') are soft neutrosophic N-ideals of soft neutrosophic N-LA-semigroups (F, A) and (G, B) over neutrosophic N-LA-semigroups N(S) and N(T) respectively. Then  $(F', A') \times (G', B')$  is a soft neutrosophic N-ideal of soft neutrosophic N-LA-semigroup  $(F, A) \times (G, B)$  over  $N(S) \times N(T)$ .

**Theorem 9.** Let (F, A) be a soft neutrosophic N-LAsemigroup over S(N) and  $\{(H_j, B_j): j \in J\}$  be a non-empty family of soft neutrosophic N-ideals of (F, A). Then

1.  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic N-ideal of (F, A).

- 2.  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic N-ideal of (F, A).
- 3.  $\bigcup_{\substack{\mathcal{E} \\ j \in J}} (H_j, B_j)$  is a soft neutrosophic N-ideal of (F, A).
- 4.  $\bigvee_{j \in J} (H_j, B_j)$  is a soft neutrosophic N-ideal of (F, A).

#### 6 Soft Neutrosophic Strong N-LA-semigroup

**Definition 30.** Let  $\{S(N), *_1, *_2, ..., *_N\}$  be a neutrosophic N-LA-semigroup and (F, A) be a soft set over S(N). Then (F, A) is called soft neutrosophic strong N-LA-semigroup if and only if F(a) is a neutrosophic strong sub N-LA-semigroup of S(N) for all  $a \in A$ .

**Example 10.** Let  $S(N) = \{S_1 \cup S_2 \cup S_3, *_1, *_2, *_3\}$  be a

neutrosophic 3-LA-semigroup in Example 8. Let

 $A = \{a_1, a_2, a_3\}$  be a set of parameters. Then clearly

(F, A) is a soft neutrosophic strong 3-LA-semigroup

over S(N), where

$$F(a_1) = \{1I\} \cup \{2I, 3I\} \cup \{2I\},\$$
$$F(a_2) = \{2I\} \cup \{1I, 3I\} \cup \{2I, 3I\},\$$

**Theorem 10.** If S(N) is a neutrosophic strong N-LAsemigroup, then (F, A) is also a soft neutrosophic strong N-LA-semigroup over S(N).

**Proposition 17.** Let (F, A) and (K, D) be two soft neutrosophic strong N-LA-semigroups over S(N). Then

1. Their extended intersection  $(F, A) \cap_E (K, D)$ is soft neutrosophic strong N-LA-semigroup over S(N).

- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$  is soft neutrosophic strong N-LA-semigroup over S(N).
- 3. Their *AND* operation  $(F, A) \land (K, D)$  is soft neutrosophic strong N-LA-semigroup over S(N).

**Remark 4.** Let (F, A) and (K, D) be two soft neutrosophic strong N-LA-semigroups over S(N). Then

- 1. Their extended union  $(F, A) \cup_E (K, D)$  is not soft neutrosophic strong N-LA-semigroup over S(N).
- 2. Their restricted union  $(F, A) \cup_R (K, D)$  is not soft neutrosophic strong N-LA-semigroup over S(N).
- 3. Their *OR* operation  $(F, A) \lor (K, D)$  is not soft neutrosophic strong N-LA-semigroup over S(N).

One can easily proved (1), (2), and (3) by the help of examples.

**Definition 31.** Let (F, A) and (K, D) be two soft neutrosophic strong N-LA-semigroups over S(N). Then (K, D) is called soft neutrosophic strong sub N-LA-semigroup of (F, A), if

- 3.  $D \subseteq A$ .
- 4. K(a) is a neutrosophic strong sub N-LAsemigroup of F(a) for all  $a \in A$ .

**Theorem 11.** Let (F, A) be a soft neutrosophic strong N-

LA-semigroup over S(N) and  $\{(H_j, B_j): j \in J\}$  be a non-empty family of soft neutrosophic strong sub N-LAsemigroups of (F, A). Then

1.  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong sub N-LA-semigroup of (F, A).

- 2.  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong sub N-LA-semigroup of (F, A).
- 3.  $\bigcup_{\substack{\mathcal{E}\\ j\in J}} (H_j, B_j)$  is a soft neutrosophic strong sub N-LA-semigroup of (F, A) if  $B_j \cap B_k = \phi$ for all  $j, k \in J$ .

**Definition 32.** Let (F, A) be a soft set over a neutrosophic N-LA-semigroup S(N). Then (F, A) is called soft neutrosophic strong N-ideal over S(N) if and only if F(a) is a neutrosophic strong N-ideal of S(N) for all  $a \in A$ .

**Proposition 18.** Every soft neutrosophic strong N-ideal over a neutrosophic N-LA-semigroup is trivially a soft neutrosophic strong N-LA-semigroup but the converse is not true in general.

One can easily see the converse by the help of example.

**Proposition 19.** Let (F, A) and (K, D) be two soft neutrosophic strong N-ideals over S(N). Then

- 1. Their restricted union  $(F, A) \cup_R (K, D)$  is not a soft neutrosophic strong N-ideal over S(N).
- 2. Their restricted intersection  $(F, A) \cap_R (K, D)$  is a soft neutrosophic N-ideal over S(N).
- 3. Their extended union  $(F, A) \cup_{\varepsilon} (K, D)$  is also a not soft neutrosophic strong N-ideal over S(N).
- 4. Their extended intersection  $(F, A) \cap_{\varepsilon} (K, D)$ is a soft neutrosophic strong N-ideal over S(N).
- 5. Their *OR* operation  $(F, A) \lor (K, D)$  is a not soft neutrosophic strong N-ideal over S(N).
- 6. Their AND operation  $(F, A) \land (K, D)$  is a

soft neutrosophic strong N-ideal over S(N).

**Definition 33.** Let (F, A) and (K, D) be two soft neutrosophic strong N-LA-semigroups over S(N). Then (K, D) is called soft neutrosophic strong N-ideal of (F, A), if

- 1.  $B \subseteq A$ , and
- 2. K(a) is a neutrosophic strong N-ideal of F(a) for all  $a \in A$ .

**Theorem 12.** A soft neutrosophic strong N-ideal of a soft neutrosophic strong N-LA-semigroup over a neutrosophic N-LA\_semigroup is trivially a soft neutosophic strong sub N-LA-semigroup but the converse is not true in general.

**Theorem 13.** A soft neutrosophic strong N-ideal of a soft neutrosophic strong N-LA-semigroup over a neutrosophic N-LA\_semigroup is trivially a soft neutosophic strong Nideal but the converse is not true in general.

**Proposition 20.** If (F', A') and (G', B') are soft neutrosophic strong N-ideals of soft neutrosophic strong N-LA-semigroups (F, A) and (G, B) over neutrosophic N-LA-semigroups N(S) and N(T) respectively. Then  $(F', A') \times (G', B')$  is a soft neutrosophic strong N-ideal of soft neutrosophic strong N-LA-semigroup  $(F, A) \times (G, B)$  over  $N(S) \times N(T)$ .

**Theorem 14.** Let (F, A) be a soft neutrosophic strong

N-LA-semigroup over S(N) and  $\{(H_j, B_j): j \in J\}$ be a non-empty family of soft neutrosophic strong N-ideals

of (F, A). Then

- 1.  $\bigcap_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong Nideal of (F, A).
- 2.  $\bigwedge_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong Nideal of (F, A).

- 3.  $\bigcup_{\substack{\mathcal{E} \\ j \in J}} (H_j, B_j)$  is a soft neutrosophic strong Nideal of (F, A).
- 4.  $\bigvee_{j \in J} (H_j, B_j)$  is a soft neutrosophic strong Nideal of (F, A).

#### Conclusion

This paper we extend soft neutrosophic bisemigroup, soft neutrosophic N-semigroup to soft neutrosophic bi-LA-semigroup, and soft neutrosophic N-LA-semigroup. Their related properties and results are explained with many illustrative examples. The notions related with strong part of neutrosophy also established.

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