



A Novel Approach for Assessing the Reliability of Data Contained in a Single Valued Neutrosophic Number and its Application in Multiple Criteria Decision Making

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Abstract

Multiple criteria decision making is one of the many areas where neutrosophic sets have been successfully applied to solve various problems so far. Compared to a fuzzy set, and similar sets, neutrosophic sets use more membership functions which makes them suitable for using complex evaluation criteria in multiple criteria decision making. On the other hand, the application of three membership functions makes evaluation somewhat more complex compared to evaluation using fuzzy sets. The reliability of the data used to solve a problem can have an impact on the selection of the appropriate solution/alternative. Therefore, this paper discusses an approach that can be used to assess the reliability of information collected by surveying respondents. The usability of the proposed approach is demonstrated in the numerical illustration of the supplier selection.

Keywords: neutrosophy, reliability, single-valued neutrosophic numbers, decision-making.

1. Introduction

Multiple criteria decision making (MCDM) started to emerge about 50 years ago, and until now it is used for solving a number of different decision-making problems in different fields. MCDM can be defined as making choices in the presence of multiple conflicting criteria [1-3]. Solving complex decision-making problems is usually associated with the need to use a larger number of criteria or use of more complex criteria that are later decomposed into sub-criteria [4-5]. However, an increase in the number of criteria, as well as sub-criteria, can be less desirable in cases where data should be collected by the survey [6].

Significant progress in using the MCDM methods for solving complex decision-making problems was made after Zadeh [7] proposed fuzzy sets, on which basis Bellman and Zadeh [8] proposed fuzzy MCDM [9-10]. Since then, many extensions of fuzzy sets theory have been developed, such as: interval-valued fuzzy sets [11], intuitionistic fuzzy sets [12] and bipolar fuzzy sets [13]. In 1999, Smarandache [14] introduced the concept of neutrosophic sets, as a generalization of the fuzzy sets theory and their extensions.

So far, neutrosophic sets are successfully used in the area of multi-criteria decision-making. Many extensions of the MCDM methods are proposed based on the use of neutrosophic numbers, such as: neutrosophic AHP [15]; neutrosophic TOPSIS [1]; neutrosophic MULTIMOORA [16]; neutrosophic WASPAS [17]; neutrosophic PROMETHEE [18]; neutrosophic VIKOR [19]; neutrosophic ARAS [20]; neutrosophic GRA [21]; neutrosophic EDAS [22], and so forth. Besides, it is worth mentioning newly-developed approaches, such as: the importance of neutrosophic soft matrices in decision-making [23], interval-valued neutrosophic soft sets in decision-making [24], as well as ivnpiv-neutrosophic soft sets for decision-making [25]. In general, neutrosophy so far is used in solving a number of decision-making problems [26-32].

Fuzzy sets theory introduces partial membership to a set, expressed by membership function $\mu_{(x)}$, where membership function can have different forms, such as: bell-shaped, triangular, trapezoidal and singleton. Some other extensions of fuzzy sets theory introduced other membership functions such as: a non-membership function $\nu_{(x)}$, a positive membership function $\mu_{(x)}^+$ and a negative membership function $\nu_{(x)}^+$. Neutrosophic sets theory introduces three membership functions that can be used to describe belonging to a set, that is; truth membership, indeterminacy membership, falsity membership. That is why neutrosophic sets could be more suitable for evaluating complex phenomena, events and problems.

However, the use of three membership functions can make evaluation somewhat more complex compared to evaluation using fuzzy sets. Therefore Smarandache *et al.* [33] proposed an approach that can be used to assess the reliability of information collected by surveying respondents. This approach is reviewed again in this article, and a new approach for determining the reliability of information contained in single valued neutrosophic numbers is also presented.

Therefore, the remainder of the article is organized as follows: in Section 2 basic elements of neutrosophic sets and single-valued neutrosophic numbers are considered. In Section 3 approaches for ranking single valued neutrosophic numbers are considered, and in Section 4 a numerical illustration is given in order to demonstrate the proposed approach. Finally, conclusions are given.

2. Basic Elements of Neutrosophic Sets and Single Valued Neutrosophic Numbers

Definition 1. Let X be a nonempty set, with a generic element in X denoted by x . Then, the Neutrosophic Set (NS) A in X is as follows [14]:

$$A = \left\{ \left\langle x, T_A(x), I_A(x), F_A(x) \right\rangle \middle| x \in X \right\}, \quad (1)$$

with: $T_A : X \rightarrow]^{-}0, 1^{+}[$; $I_A : X \rightarrow]^{-}0, 1^{+}[$; $F_A : X \rightarrow]^{-}0, 1^{+}[$ and $^{-}0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3^{+}$

where: $T_A(x)$, $I_A(x)$ and $F_A(x)$ are the truth-membership function, the indeterminacy-membership function and the falsity-membership function, respectively.

Definition 2. Let X be a nonempty set. The Single Valued Neutrosophic Set (SVNS) A in X is as follows [14, 34]:

$$A = \left\{ \left\langle x, T_A(x), I_A(x), F_A(x) \right\rangle \middle| x \in X \right\}, \quad (2)$$

with: $T_A : X \rightarrow [0, 1]$; $I_A : X \rightarrow [0, 1]$; $F_A : X \rightarrow [0, 1]$ and $0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3$.

Definition 3. For an SVNS A in X , the triple $\langle t_A, i_A, f_A \rangle$ is called the Single Valued Neutrosophic Number (SVNN) [14, 34].

Definition 4. Let $X_i = \langle t_i, i_i, f_i \rangle$ be a collection of SVNNs and $x = \langle t_x, i_x, f_x \rangle$ a SVNN; then the Hamming distance $h_{(x)}$ between x and the ideal point $x^+ = \langle t^+, i^+, f^+ \rangle = \langle \max_i t_i, \min_i i_i, \min_i f_i \rangle$ is as follows:

$$h_{(x)} = \frac{1}{3} \left(|t^+ - t_x| + |i^+ - i_x| + |f^+ - f_x| \right). \tag{3}$$

Definition 5. Let $A_j = \langle t_j, i_j, f_j \rangle$ be a collection of SVNNs and $W = (w_1, w_2, \dots, w_n)^T$ be an associated weighting vector. Then the Single Valued Neutrosophic Weighted Average (SVNWA) operator of A_j is as follows [35]:

$$SVNWA(A_1, A_2, \dots, A_n) = \sum_{j=1}^n w_j A_j = \left(1 - \prod_{j=1}^n (1 - t_j)^{w_j}, \prod_{j=1}^n (i_j)^{w_j}, \prod_{j=1}^n (f_j)^{w_j} \right). \tag{4}$$

where: w_j is the element j of the weighting vector, $w_j \in [0, 1]$ and $\sum_{j=1}^n w_j = 1$.

3. Determining the Reliability of the Information Contained in Single Valued Neutrosophic Numbers

Smarandache *et al.* [33] proposed an approach for accessing the reliability of the information $r_{(x)}$ contained in a SVNN, as follows:

$$r_{(x)} = \frac{t - f}{1 + i}, \tag{5}$$

where: t, i, f denote the truth, the intermediacy and the falsity of information contained in SVNN $x = \langle t, i, f \rangle$, $r \in [-1, 1]$.

Example: Assume that $x = \langle 0.9, 0.1, 0.3 \rangle$ is a SVNN. Then, the reliability of x is $r_{(x)} = \frac{0.9 - 0.3}{1 + 0.1} = 0.55$

In this approach, it is proposed to calculate reliability as follows:

$$r_{(x)} = \begin{cases} \frac{|t - f|}{t + i + f} & t + i + f \neq 0 \\ 0 & t + i + f = 0 \end{cases}, \tag{6}$$

where: $r \in [0, 1]$.

Example: Assume that $x = \langle 0.9, 0.1, 0.3 \rangle$ is a SVNN. Then, the reliability of x is $r_{(x)} = \frac{|0.9 - 0.3|}{0.9 + 0.1 + 0.3} = 0.46$

One comparison of the reliability calculated using Eq. (5) and Eq. (6) for some characteristic values of t, i and f is shown in Table 1.

Table 1. The reliability calculated using Eq. (5) and Eq. (6)

t	i	f	Eq. (5)	Eq. (6)
1	0	0	1	1
0	0	1	-1	1
1	0	1	0	0
1	1	0	0.5	0.5
0	1	1	-0.5	0.5
1	1	1	0	0
0	0	0	0	0

It can be seen from Table 1, Eq. (5) provides values from the interval $[-1, 1]$, with a value of zero being the least desirable. Equation (6) provides values from the interval $[0, 1]$ where a higher value of the reliability function is more desirable.

4. A Numerical illustration

In order to briefly demonstrate the usability of the SVNNS for solving MCDM problems, an example of supplier selection is presented in this section. Assume that one company has to consider engaging with a new supplier. Therefore, a team of three experts is formed with the aim to select the most appropriate supplier from three alternatives, denoted as $A_1 - A_3$, on the basis on the following criteria:

- C_1 – Delivery,
- C_2 – Quality,
- C_3 – Flexibility,
- C_4 – Service, and
- C_5 – Price.

The ratings obtained from three experts are shown in Tables 1 to 3.

Table 2. The ratings obtained from the first of three experts

	C_1	C_2	C_3	C_4	C_5
A_1	<0.9, 0.10, 0.30>	<0.7, 0.2, 0.3>	<0.6, 0.0, 0.0>	<0.7, 0.0, 0.0>	<0.5, 0.0, 0.1>
A_2	<0.8, 0.00, 0.00>	<0.8, 0.0, 0.1>	<0.8, 0.0, 0.0>	<0.8, 0.0, 0.0>	<0.8, 0.0, 0.0>
A_3	<0.7, 0.00, 0.00>	<0.5, 0.0, 0.0>	<0.6, 0.0, 0.0>	<0.6, 0.0, 0.0>	<0.7, 0.2, 0.0>
A_4	<0.8, 0.10, 0.10>	<0.6, 0.0, 0.0>	<0.7, 0.0, 0.3>	<0.5, 0.2, 0.2>	<0.5, 0.0, 0.0>

Table 3. The ratings obtained from the second of three experts

	C_1	C_2	C_3	C_4	C_5
A_1	<0.6, 0.00, 0.10>	<0.7, 0.0, 0.1>	<0.6, 0.0, 0.0>	<0.5, 0.0, 0.0>	<0.2, 0.0, 0.9>
A_2	<0.8, 0.00, 0.30>	<0.6, 0.0, 0.1>	<0.7, 0.0, 0.0>	<0.8, 0.0, 0.2>	<0.1, 0.0, 0.8>
A_3	<0.7, 0.00, 0.30>	<0.8, 0.0, 0.0>	<0.7, 0.0, 0.0>	<0.6, 0.0, 0.4>	<0.3, 0.0, 0.2>
A_4	<0.6, 0.00, 0.20>	<0.7, 0.1, 0.2>	<0.7, 0.0, 0.0>	<0.6, 0.0, 0.4>	<0.5, 0.0, 0.1>

Table 4. The ratings obtained from the third of three experts

	C_1	C_2	C_3	C_4	C_5
A_1	<0.8, 0.20, 0.20>	<0.6, 0.0, 0.4>	<0.5, 0.0, 0.0>	<0.6, 0.0, 0.1>	<0.8, 0.0, 0.4>
A_2	<0.6, 0.10, 0.10>	<0.6, 0.2, 0.4>	<0.8, 0.1, 0.0>	<0.5, 0.0, 0.1>	<0.7, 0.0, 0.0>
A_3	<0.6, 0.00, 0.00>	<0.7, 0.0, 0.3>	<0.6, 0.1, 0.0>	<0.6, 0.0, 0.0>	<0.5, 0.1, 0.3>
A_4	<0.7, 0.00, 0.00>	<0.8, 0.0, 0.2>	<0.7, 0.0, 0.0>	<0.6, 0.0, 0.1>	<0.6, 0.0, 0.0>

The reliability of ratings obtained using Eq. (5) and Eq. (6) are shown in Tables 5 and 6. The average reliability of all ratings are also shown in Tables 5 and 6.

Table 5. The reliability of ratings obtained from the first expert using Eq. (5)

	C_1	C_2	C_3	C_4	C_5
A_1	0.55	0.33	0.60	0.70	0.40
A_2	0.80	0.70	0.80	0.80	0.80
A_3	0.70	0.50	0.60	0.60	0.58
A_4	0.64	0.60	0.40	0.25	0.50
	Avg				0.59

Table 6. The reliability of ratings obtained from the first expert using Eq. (6)

	C_1	C_2	C_3	C_4	C_5
A_1	0.46	0.33	1.00	1.00	0.67
A_2	1.00	0.78	1.00	1.00	1.00
A_3	1.00	1.00	1.00	1.00	0.78
A_4	0.70	1.00	0.40	0.33	1.00
	Avg				0.82

The average reliability of responses obtained from all three decision makers, calculated using Eq. (6), are accounted for in Table 7.

Table 7. The average reliability of ratings obtained from all experts using Eq. (6)

Reliability	
E_1	0.82
E_2	0.65
E_3	0.69

As can be seen from Table 7, all three experts provide relatively consistent responses, and therefore their ratings can be used for further evaluation of alternatives. In contrast, if the average reliability of ratings obtained from a respondent has low value, his or her responses must be rejected from further evaluation of the alternatives or his or her responses must be re-considered again until adequate reliability is achieved.

A possible scenario of the evaluation of alternatives is discussed below. A group decision matrix, shown in Table 8, is constructed using Eq. (4) and the following weights $w_j = \left(\frac{1}{3}, \frac{1}{3}, \frac{1}{3}\right)$. The overall ratings are calculated using Eq. (4) and the following weighting vector $w_j = (0.19, 0.22, 0.19, 0.18, 0.22)$, as it is shown in Table 9. The ideal point is also shown in Table 9.

Table 8. The group decision matrix

	C_1	C_2	C_3	C_4	C_5
w_j	0.19	0.22	0.19	0.18	0.22
A_1	<0.80, 0.1, 0.20>	<0.67, 0.1, 0.28>	<0.57, 0.0, 0.00>	<0.61, 0.0, 0.03>	<0.57, 0.0, 0.62>
A_2	<0.75, 0.0, 0.14>	<0.68, 0.1, 0.21>	<0.77, 0.0, 0.00>	<0.73, 0.0, 0.10>	<0.62, 0.0, 0.41>
A_3	<0.67, 0.0, 0.11>	<0.69, 0.0, 0.11>	<0.64, 0.0, 0.00>	<0.60, 0.0, 0.16>	<0.53, 0.1, 0.18>
A_4	<0.71, 0.0, 0.10>	<0.71, 0.0, 0.14>	<0.70, 0.0, 0.11>	<0.57, 0.1, 0.24>	<0.54, 0.0, 0.03>

Table 9. The overall ratings and ideal point

Overall ratings	
A_1	<0.65, 0.00, 0.00>
A_2	<0.71, 0.00, 0.00>
A_3	<0.63, 0.00, 0.00>
A_4	<0.65, 0.00, 0.10>
A^+	<0.71, 0.00, 0.00>

Finally, the ranking results, obtained using Eq. (3), are encountered for in Table 10.

Table 10. The ranking results

	$h_{(i)}$	Rank
A_1	0.0063	2
A_2	0.0000	1
A_3	0.0092	3
A_4	0.0179	4

As can be seen from Table 10, the most appropriate alternative is alternative denoted as A_2 .

5. Conclusion

Neutrosophic sets theory introduces three membership functions that is why single-valued neutrosophic numbers could be suitable for evaluating alternatives in relation to the complex evaluation criteria in multiple criteria decision making. However, the use of three membership functions can make evaluation somewhat complex especially when the evaluation is based on data collected by the survey.

The reliability of the data used to solve a problem can have an impact on the final selection of the appropriate alternative. In this manuscript, an improved procedure for estimating the reliability of the collected data is proposed.

Therefore, Smarandache et al. [33] has proposed an approach that can be used to assess the reliability of information collected by surveying respondents.

Compared to the previous approach, in the new approach reliability and information belong to the interval $[0, 1]$, unlike the previously proposed approach where reliability belongs to the interval $[-1, 1]$, which makes new application easier for using.

By using the proposed procedure, the reliability of data could be easily determined. In this paper, the usability and efficiency of the proposed approach is successfully demonstrated on an illustrative example of the supplier selection.

Funding: The research presented in this article was done with the financial support of the Ministry of Education, Science and Technological Development of the Republic of Serbia, as part of the financing of scientific research at the University of Belgrade, Technical Faculty in Bor.

Conflicts of Interest: “The authors declare no conflict of interest.”

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