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# The neutrosophic strongly open maps in neutrosophic bi-topological spaces 

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#### Abstract

In this work, some new classes of neutrosophic (1,2)-maps are investigated and discussed their basic attributions in neutrosophic bi-topological space (NBTS). In this paper, the relationships among these classes like neutrosophic (1,2)-continuous/ open/ strongly open/ generality open/ maps are discussed. Moreover, our work in this paper is examined and some examples are shown to support this research.


## Subject Classification: 06D72, 03E72.

Keywords: Neutrosophic sets, Bi-topological spaces, (1,2)-continuous maps, (1,2)-open maps.

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## 1. Introduction

The connotations of the maps in bi-topological spaces have been discussed and explained extensively in general topology see ([3], [4]). After that, some applications in general topology and non-classical topology like soft bi-topological spaces are discussed see ([5], [6]). Smarandache [7] presented the neutrosophic set / logic/ probability/ statistics, the neutrosophic set is studied in topology, algerbra and other fields. It is one of the non-classical sets, like fuzzy, nano, soft and so on, see ([8]-[35]). Next, some applications of neutrosophic set are studied see ([36]). In 2014, the connotations of "neutrosophic closed set" and "neutrosophic continuous function" are given [37]. In this work, some new classes of neutrosophic (1,2)-maps are investigated and discussed their basic attributions in (NBTS). In this paper, the relationships among these classes like neutrosophic (1,2)-continuous/open/strongly open/ generality open/ maps are discussed. Moreover, our work in this paper is examined and some examples are shown to support this research.

## 2. Preliminaries

Definition 2.1 : [1] Assume $\Psi \neq \varphi$. A neutrosophic set (NS) $\theta$ is defined as $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ where $\partial_{\sigma}(\alpha)$ is the degree of membership, $\omega_{\theta}(\alpha)$ is the degree of indeterminacy and $\ell_{\theta}(\alpha)$ is the degree of non-membership, $\forall \alpha \in \Psi$ to $\theta$.

Definition 2.2 [1] Assume $\theta$ and $\beta$ are neutrosophic sets (NSs) as following
$\theta=\left\langle\alpha, \partial_{\bar{\sigma}}(\alpha), \quad \omega_{\theta}(\alpha), \quad \ell_{\theta}(\alpha): \quad \alpha \in \Psi\right\rangle \quad$ and $\beta=\left\langle\alpha, \partial_{\beta}(\alpha), \quad \omega_{\beta}(\alpha)\right.$, $\left.\ell_{\beta}(\alpha): \alpha \in \Psi\right\rangle$. Then
(1) $\theta \subseteq \beta$ if and only if $\partial_{\bar{\sigma}}(\alpha) \leq \partial_{\chi}(\alpha), \quad \omega_{\theta}(\alpha) \geq \omega_{\chi}(\alpha)$ and $\ell_{\theta}(\alpha) \geq$ $\ell_{\chi}(\alpha)$,
(2) $\theta^{c}=\left\langle\alpha, \ell_{\theta}(\alpha), 1-\omega_{\theta}(\alpha), \partial_{\theta}(\alpha): \alpha \in \Psi\right\rangle$,
(3) $\theta \cup \beta=\left\langle\alpha, \partial_{\theta}(\alpha) \vee \partial_{\beta}(\alpha), \omega_{\theta}(\alpha) \wedge \omega_{\beta}(\alpha), \ell_{\theta}(\alpha) \wedge \ell_{\beta}(\alpha): \alpha \in \Psi\right\rangle$,
(4) $\theta \cap \beta=\left\langle\alpha, \partial_{\theta}(\alpha) \wedge \partial_{\beta}(\alpha), \omega_{\theta}(\alpha) \vee \omega_{\beta}(\alpha), \ell_{\theta}(\alpha) \vee \ell_{\beta}(\alpha): \alpha \in \Psi\right\rangle$.

Definition 2.3 : [1] $1_{N}$ and $0_{N}$ are of the form $0_{N}=\{\langle\alpha,(0,1,1)\rangle: \alpha \in \Psi\}$ and $1_{N}=\{\langle\alpha,(1,0,0)\rangle: \alpha \in \Psi\}$.

Definition 2.4 : [2] We say ( $\Psi, \tau$ ) is a neutrosophic topological space (NTS) if and only if $\tau$ is a collection of (NSs) in $\Psi$ and it such that:
(1) $1_{N}, 0_{N} \in \tau$,
(2) $\theta \cap \beta \in \tau$ for any $\theta, \beta \in \tau$,
(3) $\bigcup_{i \in I} \theta_{i} \in \tau$ for any arbitrary family $\left\{\theta_{i} \mid i \in I\right\} \subseteq \tau$.

Also, any $\theta \in \tau$ is called neutrosophic open set (NOS) and we say neutrosophic closed set (NCS) for its complement.

Definition 2.5 : [2] The neutrosophic closure of (NS) $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha)\right.$, $\left.\ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ is the intersection of all (NCS) containing $\theta$ and is referred by $\operatorname{Ncl}(\theta)$. While the neutrosophic interior of $\theta$ is the union of all (NOS) is contained in $\theta$ and is referred by $N \operatorname{int}(\theta)$.

Definition 2.6: [2] For any (NS) $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ in (NTS) $(\Psi, \tau)$ we say that $\theta$ is a neutrosophic semi-open set (NSOS) if there exists (NOS) $\beta=\left\langle\alpha, \partial_{\beta}(\alpha), \omega_{\beta}(\alpha), \ell_{\beta}(\alpha): \alpha \in \Psi\right\rangle$ such that $\beta \subseteq \theta \subseteq \operatorname{Ncl}(\theta)$.

## 3. Neutrosophic Strongly Open Maps:

In this section, the connotations of neutrosophic (1, 2)-strongly/ generality/ open maps are investigated and their relations with neutrosophic (1, 2)-open/continuous maps are stated. Some of their applications are given. Moreover, the current work is supported by a number of examples.

Definition 3.1: Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a neutrosophic map (NM) from a neutrosophic bi-topological space (NBTS) ( $\Psi, \tau_{1}, \tau_{2}$ ) into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right), \xi$ is called a neutrosophic (1,2)- continuous map (N-(1,2)-CM) if $\xi^{-1}(\beta)$ is neutrosophic (1,2)-open set ( $\left.\mathrm{N}-(1,2)-\mathrm{OS}\right)$ in $\left(\Psi, \tau_{1}, \tau_{2}\right)$ for any $(\mathrm{N}-(1,2)-\mathrm{OS}) \beta=\left\langle\varsigma, \partial_{\beta}(\varsigma), \omega_{\beta}(\varsigma), \quad \ell_{\beta}(\varsigma): \varsigma \in \Omega\right\rangle$ in $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$.

Definition 3.2 : Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a (NM) from a (NBTS) ( $\Psi, \tau_{1}, \tau_{2}$ ) into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right), \xi$ is called a neutrosophic (1, 2)- open map ( $\mathrm{N}-(1,2)-\mathrm{OM})$ if $\xi(\beta)$ is ( $\mathrm{N}-(1,2)-\mathrm{OS})$ in $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ for any ( $\mathrm{N}-(1,2)-\mathrm{OS}$ ) $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ in $\left(\Psi, \tau_{1}, \tau_{2}\right)$.

Definition 3.3 : Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a (NM) from a (NBTS) $\left(\Psi, \tau_{1}, \tau_{2}\right)$ into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right), \xi$ is called a neutrosophic ( 1 , 2)-strongly open map ( $\mathrm{N}-(1,2)-\mathrm{SOM}$ ) if $\xi(\theta) \in \lambda_{1} \cup \lambda_{2}$ for any (NSOS) $\theta=\left\langle\alpha, \partial_{\bar{\sigma}}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ in $\left(\Psi, \tau_{1} \cap \tau_{2}\right)$.

Example 3.4 : Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a (NM) from a (NBTS) ( $\left.\Psi, \tau_{1}, \tau_{2}\right)$ into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$, where $\lambda_{1}$ or $\lambda_{2}$ is a neutrosophic discrete topology (NDT). Hence, $\lambda_{1} \cup \lambda_{2}=N S(\Omega)$, where $N S(\Omega)$ is the family of all the (NSs) in $\Omega$. Hence, for any (NSOS) $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ in ( $\Psi, \tau_{1} \cap \tau_{2}$ ) we have $\xi(\theta) \in \lambda_{1} \cup \lambda_{2}$ and this implies that $\xi$ is a ( $\mathrm{N}-(1,2)-$ SOM).

Remark 3.5 : It is easy to show that each ( $\mathrm{N}-(1,2)-\mathrm{SOM})$ is ( $\mathrm{N}-(1,2)-\mathrm{OM})$. However, the converse is not necessary true in general.

Example 3.6 : Let $\Psi=\left\{s_{1}, s_{2}, s_{3}\right\}, \tau_{1}=\left\{1_{N}, 0_{N}, \theta\right\}, \tau_{2}=\left\{1_{N}, 0_{N}, \theta, \beta\right\}$, wher e $\theta=\left\{\left\langle s_{1}, 0.5,0.1,0.6\right\rangle,\left\langle s_{2}, 0.3,0.3,0.5\right\rangle,\left\langle s_{3}, 0.3,0.4,0.7\right\rangle\right\}$ a n d $\beta=\left\{\left\langle s_{1}, 0.7,0.1,0.2\right\rangle,\left\langle s_{2}, 0.6,0.2,0.1\right\rangle,\left\langle s_{3}, 0.9,0.3,0.2\right\rangle\right\} \quad$ let $\Omega=\left\{a_{1}, a_{2}, a_{3}\right\}$ $\lambda_{1}=\lambda_{2}=\left\{1_{N}, 0_{N}, C, D, E\right\}, \quad$ where $\quad C=\left\{\left\langle a_{1}, 0.6,0.2,0.7\right\rangle,\left\langle a_{2}, 0.4,0.4,0.6\right\rangle\right.$, $\left.\left\langle a_{3}, 0.4,0.5,0.8\right\rangle\right\}, \quad D=\left\{\left\langle a_{1}, 0.8,0.2,0.3\right\rangle,\left\langle a_{2}, 0.7,0.3,0.2\right\rangle,\left\langle a_{3}, 0.8,0.4,0.3\right\rangle\right\}$, and $\quad E=\left\{\left\langle a_{1}, 0.9,0.1,0.2\right\rangle,\left\langle a_{2}, 0.8,0.2,0.1\right\rangle,\left\langle a_{3}, 0.9,0.3,0.3\right\rangle\right\}$. Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a (NM), where $\xi\left(s_{1}\right)=a_{1}, \xi\left(s_{2}\right)=a_{2}$ and $\xi\left(s_{3}\right)=a_{3}$. Then $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ is a (N-(1,2)-OM) butnot(N-(1,2)SOM), since there is a (NSOS) $H$ in $\left(\Psi, \tau_{1} \cap \tau_{2}\right)$ where $H=\left\{\left\langle s_{1}, 0.5,0.1,0.6\right\rangle\right.$, $\left.\left\langle s_{2}, 0.4,0.1,0.1\right\rangle,\left\langle s_{3}, 0.5,0.3,0.6\right\rangle\right\}$, but $\quad \xi(H)=T \notin \lambda_{1} \cup \lambda_{2}$, where $T=\left\{\left\langle a_{1}, 0.5,0.1,0.6\right\rangle,\left\langle a_{2}, 0.4,0.1,0.1\right\rangle,\left\langle a_{3}, 0.5,0.3,0.6\right\rangle\right\}$.

Theorem 3.7: If $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ is $(N-(1,2)-O M)$ from neutrosophic discrete bi-topological space (NDBTS) $\left(\Psi, \tau_{1}, \tau_{2}\right)$ into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$, then $\xi$ is ( $N$-(1,2)-SOM).

Proof: suppose $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ is (NSOS) in $\left(\Psi, \tau_{1}, \tau_{2}\right)$ we consider that $\theta$ is $(\mathrm{N}-(1,2)-\mathrm{OS})$ in $\left(\Psi, \tau_{1}, \tau_{2}\right)$ [since $\left(\Psi, \tau_{1}, \tau_{2}\right)$ is (NDBTS)]. Therefore, $\xi(\theta)$ is ( $\mathrm{N}-(1,2)-\mathrm{OS})$ in $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ [since $\xi$ is ( N - $(1$, 2)-OM)], so $\boldsymbol{\xi}$ is ( $\mathrm{N}-(1,2)-\mathrm{OM})$.

Definition 3.8: Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a (NM) from a (NBTS) $\left(\Psi, \tau_{1}, \tau_{2}\right)$ into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right), \xi$ is called a neutrosophic (1, 2)-generality open map ( $\mathrm{N}-(1,2)-\mathrm{GOM})$ if $\xi(\theta)$ is (NSOS) in $\left(\Psi, \tau_{1} \cap \tau_{2}\right)$ for each $\theta=\left\langle\alpha, \partial_{\bar{\sigma}}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle(\mathrm{NSOS})$ in $\left(\Psi, \tau_{1} \cap \tau_{2}\right)$.

Example 3.9 : Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ be a (NM) from a (NBTS) ( $\Psi, \tau_{1}, \tau_{2}$ ) onto (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$, where $\tau_{1}$ or $\tau_{2}$ is a neutrosophic indiscrete topology (NIT), we have $\tau_{1} \cap \tau_{2}=\left\{1_{N}, 0_{N}\right\}$. Therefore, for any (NSOS) $\theta=\left\langle\alpha, \partial_{\sigma}(\alpha), \omega_{\theta}(\alpha), \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ in $\left(\Psi, \tau_{1} \cap \tau_{2}\right)$ we have $\theta=0_{N}$ or $1_{N}$ and this implies that $\xi(\theta)=0_{N}$ or $1_{N}$ and hence $\xi$ is a ( N -(1,2)-GOM).

Remark 3.10 : It is easy to show that each ( $\mathrm{N}-(1,2)-\mathrm{SOM})$ is ( $\mathrm{N}-(1,2)-\mathrm{GOM})$. However, the converse is not necessary true in general.

Example 3.11 : take $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ in Example (3.6), we obtain $\xi$ is a ( $\mathrm{N}-(1,2)-\mathrm{OM}$ ) but not ( $\mathrm{N}-(1,2)-\mathrm{SOM})$. For any (NSOS) $\theta$ in ( $\Psi, \tau_{1} \cap \tau_{2}$ ), we have there exists (NOS) $\beta$ in ( $\Psi, \tau_{1} \cap \tau_{2}$ ) satisfies $\beta \subseteq \theta$ $\subseteq \operatorname{Ncl}(\beta)$. But, $\beta \in \tau_{1} \cap \tau_{2}$, thus $\beta$ can be formed by union of two (NOSs) $\beta \in \tau_{1}$ and $\beta \in \tau_{2}$. Hence $\beta$ is ( $\mathrm{N}-(1,2)$-OS) in ( $\left.\Psi, \tau_{1}, \tau_{2}\right)$. Therefore $\xi(\beta)$ is ( $\mathrm{N}-(1,2)-\mathrm{OS})$ in $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ [since $\xi$ is a (N-(1,2)-OM)]. Also, $\xi(\beta) \subseteq$ $\xi(\theta) \subseteq \xi(\operatorname{Ncl}(\beta)) \subseteq \operatorname{Ncl}(\xi(\beta))$. But $\xi(\beta) \in \lambda_{1} \cap \lambda_{2}$ then $\xi(\theta)$ is (NSOS)in $\left(\Omega, \lambda_{2} \cap \lambda_{2}\right)$. Hence $\xi$ is ( $\left.\mathrm{N}-(1,2)-\mathrm{GOM}\right)$ but not ( $\left.\mathrm{N}-(1,2)-\mathrm{SOM}\right)$.

Theorem 3.12: If $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ is $(N-(1,2)-O M)$ and $(N-(1,2)$ $C M)$, then $\xi$ is ( $N-(1,2)-G O M)$.

Proof : Let $\xi:\left(\Psi, \tau_{1}, \tau_{2}\right) \rightarrow\left(\Omega, \lambda_{1}, \lambda_{2}\right) \quad$ be a $(\mathrm{N}-(1,2)-\mathrm{CM})$ and (N-(1,2)-OM) from a (NBTS) ( $\left.\Psi, \tau_{1}, \tau_{2}\right)$ into (NBTS) $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$, suppose $\theta=\left\langle\alpha, \partial_{\bar{\sigma}}(\alpha), \omega_{\theta}(\alpha), \quad \ell_{\theta}(\alpha): \alpha \in \Psi\right\rangle$ is (NSOS) in $\left(\Omega, \lambda_{2} \cap \lambda_{2}\right)$, then there exists (NOS) $\beta$ in $\left(\Omega, \lambda_{2} \cap \lambda_{2}\right)$ satisfies: $\beta \subseteq \theta \subseteq \operatorname{Ncl}(\beta) \Rightarrow$ $\xi(\beta) \subseteq \xi(\theta) \subseteq \xi(\operatorname{Ncl}(\beta))$. In other side, the (NOS) $\beta$ is a (N-(1,2)-OS) in bi-topological space ( $\Psi, \tau_{1}, \tau_{2}$ ) since $\beta \in \tau_{1} \cap \tau_{2}$, we consider that $\xi(\operatorname{Ncl}(\beta)) \subseteq \operatorname{Ncl}(\xi(\beta)) \quad[$ since $\xi$ is $(\mathrm{N}-(1,2)-\mathrm{CM})]$. Moreover, $\xi(\theta)$ is ( $\mathrm{N}-(1,2)-\mathrm{OS}$ ) in $\left(\Omega, \lambda_{1}, \lambda_{2}\right)$ [since $\xi$ is ( $\left.\mathrm{N}-(1,2)-\mathrm{OM}\right)$ ], Then $\xi(\theta)$ is (NSOS) in $\left(\Omega, \lambda_{2} \cap \lambda_{2}\right)$. Therefore, $\xi$ is ( $\left.\mathrm{N}-(1,2)-\mathrm{GOM}\right)$.

Remark 3.13 : We can explain our results by this diagram:


Figure 1
The relationships among four classes of the neutrosophic (1,2)-maps

## 4. Conclusion

In this work, attempt has been made to apply the notion of neutrosophic maps to study some types in (NBTSs) like; neutrosophic (1,2)-continuous/ open/ strongly open/ generality open/ maps. Moreover, the properties of these new notions are investigated. We will use the soft sets theory in future work to investigate new classes of neutrosophic soft maps and then we can disuse their applications in neutrosophic soft bi- topological spaces.

## References

[1] F. Smarandache, Neutrosophy and Neutrosophic Logic, First International Conference on Neutrosophy, Neutrosophic Logic, Set, Probability and Statistics, University of New Mexico: Gallup, NM, USA, (2002).
[2] A. A. Salama and S. A. Alblowi, Neutrosophic Set and Neutrosophic Topological Spaces, IOSRJ. Math., 3, (2012) 31-35.
[3] J. C. Kelly, Bitopological Spaces, Proceedings of the London Mathematical Society, 13(1), (1963), 71-89.
[4] B. Bhattacharya and A. Paul, On bitopological $\gamma$-open set, Iosr Journal of Mathematics, 5(2), (2013), 10-14.
[5] B. M. Ittanagi, Soft Bitopological Spaces, International Journal of Computer Applications, 107(7), (2014), 1-4.
[6] A. M. Al -Musawi, S. M Khalil, M. A. Ulrazaq, Soft (1,2)-Strongly Open Maps in Bi-Topological Spaces, IOP Conference Series: Materials Science and Engineering, 571 (2019) 012002, doi:10.1088/1757899X/571/1/012002.
[7] F. Smarandache, A Unifying Field in Logics: Neutrosophic Logic. Neutrosophy, Neutrosophic Set, Neutrosophic Probability; American Research Press: Rehoboth, NM, USA, 1999.
[8] S. M. Khalil, \& F. H. Khadhaer, An algorithm for the generating permutation algebras using soft spaces. Journal of Taibah University for Science, 12(3), (2018), 299-308.
[9] S. M. Khalil, M. H. Hasab, Decision Making Using New Distances of Intuitionistic Fuzzy Sets and Study Their Application in The Universities, INFUS, Advances in Intellgent Systems and Computing, (2020), doi.org/10.1007/978-3-030-51156-2_46.
[10] S. M. Khalil and A. Rajah, Solving the Class Equation $x^{d}=\beta$ in an Alternating Group for eac $\beta \in H \cap C^{\alpha}$ and $n \notin \theta$, Journal of the Association of Arab Universities for Basic and Applied Sciences, 10,(2011), 42-50.
[11] S. M. Khalil and A. Rajah, Solving Class Equation $x^{d}=\beta$ in an Alternating Group for all $n \in \theta \quad \& \quad \beta \in H_{n} \cap C^{\alpha}$, Journal of the Association of Arab Universities for Basic and Applied Sciences, 16 (2014), 38-45.
[12] N. M. A. Abbas and S. M. Khalil, On $\alpha^{*}$-Open Sets in Topological Spaces, IOP Conference Series: Materials Science and Engineering, 571 (2019) 012021, doi:10.1088/1757-899X/571/1/012021.
[13] S. M. Khalil, The Permutation Topological Spaces and their Bases, Basrah Journal of Science (A), 32(1), (2014), 28-42.
[14] S. M. Khalil and N. M. A. Abbas, On Nano with Their Applications in Medical Field, AIP Conference Proceedings 2290, 040002 (2020); https:/ /doi.org/10.1063/5.0027374
[15] S. M. Khalil, New category of the fuzzy d-algebras, Journal of Taibah University for Science, 12(2), (2018), 143-149. doi.org/10.1080/1658365 5.2018.1451059
[16] S. M. Khalil, and A. N. Hassan, New Class of Algebraic Fuzzy Systems Using Cubic Soft Sets with their Applications, IOP Conf. Series: Materials Science and Engineering, 928 (2020) 042019 doi:10.1088/1757-899X/928/4/042019
[17] S. M. Khalil and N. M. A. Abbas, Characteristics of the Number of Conjugacy Classes and P-Regular Classes in Finite Symmetric Groups, IOP Conference Series: Materials Science and Engineering, 571 (2019) 012007, doi:10.1088/1757-899X/571/1/012007.
[18] M. M. Torki and S. M. Khalil, New Types of Finite Groups and Generated Algorithm to Determine the Integer Factorization by Excel, AIP Conference Proceedings 2290, 040020 (2020); https:/ / doi. org/10.1063/5.0027691
[19] S. M. Khalil and N. M. Abbas, Applications on New Category of the Symmetric Groups, AIP Conference Proceedings 2290, 040004 (2020); https:/ /doi.org/10.1063/5.0027380
[20] S. M. Khalil and F. Hameed, Applications on Cyclic Soft Symmetric Groups, IOP Conf. Series: Journal of Physics, 1530 (2020) 012046, doi:1 0.1088/17426596/1530/1/012046.
[21] S. M. Khalil and M. Abud Alradha, Characterizations of $\rho-$ algebra and Generation Permutation Topological $\rho$-algebra Using Permutation in Symmetric Group, American Journal of Mathematics and Statistics, 7(4), (2017), 152-159.
[22] S. M. Khalil and M. Abud Alradha, Soft Edge Algebras of the power sets, International Journal of Applications of Fuzzy Sets and Artificial Intelligence, 7, (2017), 231-243.
[23] S. M. Khalil, F. Hameed, Applications of Fuzzy $\rho$-Ideals in $\rho$ - Algebras, Soft Computing, 24(18), (2020), 13997-14004. doi. org/10.1007/s00500-020-04773-3.
[24] S. A. Abdul-Ghani, S. M. Khalil, M. Abd Ulrazaq, and A. F. Al-Musawi, New Branch of Intuitionistic Fuzzification in Algebras with Their Applications, International Journal of Mathematics and Mathematical Sciences, Volume 2018, Article ID 5712676, 6 pages.
[25] S. M. Khalil, Decision making using algebraic operations on soft effect matrix as new category of similarity measures and study their application in medical diagnosis problems, Journal of Intelligent $\mathcal{E}$ Fuzzy Systems, 37, (2019), 1865-1877. doi: 10.3233/JIFS-179249.
[26] S. M. Khalil, S. A. Abdul-Ghani, Soft M-Ideals and Soft S-Ideals in Soft S- Algebras, IOP Conf. Series: Journal of Physics, 1234 (2019) 012100, doi:10.1088/1742-6596/1234/1/012100.
[27] S. M. Khalil and F. Hameed, An algorithm for generating permutations in symmetric groups using soft spaces with general study and basic properties of permutations spaces. J Theor Appl Inform Technol, 96(9), (2018), 2445-2457.
[28] S. M. Khalil, M. Ulrazaq, S. Abdul-Ghani, Abu Firas Al-Musawi, $\sigma$-Algebra and $\sigma$-Baire in Fuzzy Soft Setting, Advances in Fuzzy Systems, Volume 2018, Article ID 5731682, 10 pages.
[29] M. A. Hasan, S. M. Khalil, and N. M. A. Abbas, Characteristics of the Soft-(1, 2) - gprw -Closed Sets in Soft Bi-Topological Spaces, IEEE, (2020), DOI: 10.1109/IT-ELA50150.2020.9253110
[30] S. M. Khalil and A. Hassan, Applications of Fuzzy Soft Ideals in Algebras, Fuzzy Information and Engineering, (2020), DOI: 10.1080/16168658.2020.1799703.
[31] S. M. Khalil, Decision Making Using New Category of Similarity Measures and Study Their Applications in Medical Diagnosis Problems, Afrika Matematika , (2021), to appear
[32] S. M. Khalil, Dissimilarity Fuzzy Soft Points and their Applications, Fuzzy Information and Engineering, 8(3), (2016), 281-294 .http:/ / dx.doi. org/10.1016/j.fiae.2016.11.003
[33] S. M. Khalil , Enoch Suleiman and Modhar M. Torki, Generated New Classes of Permutation I/B-Algebras, Journal of Discrete Mathematical Sciences and Cryptography, (2020), to appear.
[34] S. M. Saied and S. M. Khalil, Gamma Ideal Extension in Gamma Systems, Journal of Discrete Mathematical Sciences and Cryptography, (2021), to appear.
[35] K.Damodharan, M. Vigneshwaran and S. M. Khalil, $N_{\delta^{*} g \alpha}-$ Continuous and Irresolute Functions in Neutrosophic Topological Spaces, Neutrosophic Sets and Systems, 38(1), (2020). https:// digitalrepository.unm.edu/nss_journal/vol38/iss1/29
[35] V. K. Shanthi, S. Chandrasekar, K. Safina Begam, Neutrosophic Generalized Semi Closed Sets in Neutrosophic Topological Spaces, International Journal of Research in Advent Technology, 6(7), (2018), 17391943.
[36] A. A. Salama, F. Smarandache and V. Kromov, Neutrosophic Closed Set and Neutrosophic Continuous Functions, Neutrosophic Sets and Systems, 4, (2014),4-8.

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