

Neutrosophic Weakly π Generalized Continuous Mapping

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Abstract- Aim of this present paper is, we introduce and investigate about new kind of Neutrosophic continuity is called Neutrosophic weakly π generalized continuous in Neutrosophic topological spaces and also discussed about properties and characterization Neutrosophic weakly π generalized continuous

Keywords – NS $W\pi G$ open set, NS $W\pi G$ closed set Neutrosophic weakly π generalized continuous, Neutrosophic topological spaces

I. INTRODUCTION

A.A.Salama introduced Neutrosophic topological spaces by using Smarandache's Neutrosophic sets. I.Arokianani.[2] et al, introduced Neutrosophic α -closed sets.P. Ishwarya, [8]et.al, introduced and studied about on Neutrosophic semi-open sets in Neutrosophic topological spaces. Aim of this present paper is, we introduce and investigate about new kind of Neutrosophic continuity is called Neutrosophic weakly π generalized continuous in Neutrosophic topological spaces and also discussed about properties and characterization Neutrosophic weakly π generalized continuous

II. PRELIMINARIES

In this section, we introduce the basic definition for Neutrosophic sets and its operations.

Definition 2.1 [7]

Let X be a non-empty fixed set. A Neutrosophic set A is an object having the form

$$A = \{ \langle x, \eta_A(x), \sigma_A(x), \gamma_A(x) \rangle : x \in X \}$$

Where $\eta_A(x)$, $\sigma_A(x)$ and $\gamma_A(x)$ which represent Neutrosophic topological spaces the degree of membership function, the degree indeterminacy and the degree of non-membership function respectively of each element $x \in X$ to the set A .

Remark 2.2 [7]

A Neutrosophic set $A = \{ \langle x, \eta_A(x), \sigma_A(x), \gamma_A(x) \rangle : x \in X \}$ can be identified to an ordered triple

$$\langle \eta_A, \sigma_A, \gamma_A \rangle \text{ in }]-0, 1+[\text{ on } X.$$

Remark 2.3[7]

We shall use the symbol

$$A = \langle x, \eta_A, \sigma_A, \gamma_A \rangle \text{ for the Neutrosophic set } A = \{ \langle x, \eta_A(x), \sigma_A(x), \gamma_A(x) \rangle : x \in X \}.$$

Example 2.4 [7]

Every Neutrosophic set A is a non-empty set in X is obviously on Neutrosophic set having the form $A = \{ \langle x, \eta_A(x), 1 - (\eta_A(x) + \gamma_A(x)), \gamma_A(x) \rangle : x \in X \}$. Since our main purpose is to construct the tools for developing Neutrosophic set and Neutrosophic topology, we must introduce the Neutrosophic set 0_N and 1_N in X as follows:

0_N may be defined as:

$$(0_1) 0_N = \{ \langle x, 0, 0, 1 \rangle : x \in X \}$$

$$(0_2) 0_N = \{ \langle x, 0, 1, 1 \rangle : x \in X \}$$

$$(0_3) 0_N = \{ \langle x, 0, 1, 0 \rangle : x \in X \}$$

$$(0_4) 0_N = \{ \langle x, 0, 0, 0 \rangle : x \in X \}$$

1_N may be defined as :

$$(1_1) 1_N = \{ \langle x, 1, 0, 0 \rangle : x \in X \}$$

- (1₂) $1_N = \{ \langle x, 1, 0, 1 \rangle : x \in X \}$
- (1₃) $1_N = \{ \langle x, 1, 1, 0 \rangle : x \in X \}$
- (1₄) $1_N = \{ \langle x, 1, 1, 1 \rangle : x \in X \}$

Definition 2.5 [7]

Let $A = \langle \eta_A, \sigma_A, \gamma_A \rangle$ be a Neutrosophic set on X , then the complement of the set A A^c defined as

$$A^c = \{ \langle x, \gamma_A(x), 1 - \sigma_A(x), \eta_A(x) \rangle : x \in X \}$$

Definition 2.6 [7]

Let X be a non-empty set, and Neutrosophic sets A and B in the form

$$A = \{ \langle x, \eta_A(x), \sigma_A(x), \gamma_A(x) \rangle : x \in X \} \text{ and}$$

$$B = \{ \langle x, \eta_B(x), \sigma_B(x), \gamma_B(x) \rangle : x \in X \}.$$

Then we consider definition for subsets ($A \subseteq B$).

$A \subseteq B$ defined as: $A \subseteq B \Leftrightarrow \eta_A(x) \leq \eta_B(x), \sigma_A(x) \leq \sigma_B(x)$ and $\gamma_A(x) \geq \gamma_B(x)$ for all $x \in X$

Proposition 2.7 [7]

For any Neutrosophic set A , then the following condition are holds:

- (i) $0_N \subseteq A, 0_N \subseteq 0_N$
- (ii) $A \subseteq 1_N, 1_N \subseteq 1_N$

Definition 2.8 [7]

Let X be a non-empty set, and $A = \langle x, \eta_B(x), \sigma_A(x), \gamma_A(x) \rangle, B = \langle x, \eta_B(x), \sigma_B(x), \gamma_B(x) \rangle$ be two Neutrosophic sets. Then

- (i) $A \cap B$ defined as : $A \cap B = \langle x, \eta_A(x) \wedge \eta_B(x), \sigma_A(x) \vee \sigma_B(x), \gamma_A(x) \vee \gamma_B(x) \rangle$
- (ii) $A \cup B$ defined as : $A \cup B = \langle x, \eta_A(x) \vee \eta_B(x), \sigma_A(x) \wedge \sigma_B(x), \gamma_A(x) \wedge \gamma_B(x) \rangle$

Proposition 2.9 [7]

For all A and B are two Neutrosophic sets then the following condition are true:

- (i) $(A \cap B)^c = A^c \cup B^c$
- (ii) $(A \cup B)^c = A^c \cap B^c$.

Definition 2.10 [11]

A Neutrosophic topology is a non-empty set X is a family τ_N of Neutrosophic subsets in X satisfying the following axioms:

- (i) $0_N, 1_N \in \tau_N$,
- (ii) $G_1 \cap G_2 \in \tau_N$ for any $G_1, G_2 \in \tau_N$,
- (iii) $\cup G_i \in \tau_N$ for any family $\{G_i \mid i \in J\} \subseteq \tau_N$.

the pair (X, τ_N) is called a Neutrosophic topological space.

The element Neutrosophic topological spaces of τ_N are called Neutrosophic open sets.

A Neutrosophic set A is closed if and only if A^c is Neutrosophic open.

Example 2.11[11]

Let $X = \{x\}$ and

$$A_1 = \{ \langle x, 0.6, 0.6, 0.5 \rangle : x \in X \}$$

$$A_2 = \{ \langle x, 0.5, 0.7, 0.9 \rangle : x \in X \}$$

$$A_3 = \{ \langle x, 0.6, 0.7, 0.5 \rangle : x \in X \}$$

$$A_4 = \{ \langle x, 0.5, 0.6, 0.9 \rangle : x \in X \}$$

Then the family $\tau_N = \{0_N, 1_N, A_1, A_2, A_3, A_4\}$ is called a Neutrosophic topological space on X .

Definition 2.12[11]

Let (X, τ_N) be Neutrosophic topological spaces and $A = \{ \langle x, \eta_A(x), \sigma_A(x), \gamma_A(x) \rangle : x \in X \}$ be a Neutrosophic set in X .

Then the Neutrosophic closure and Neutrosophic interior of A are defined by

$$\text{Neu-cl}(A) = \cap \{K : K \text{ is a Neutrosophic closed set in } X \text{ and } A \subseteq K\}$$

$$\text{Neu-int}(A) = \cup \{G : G \text{ is a Neutrosophic open set in } X \text{ and } G \subseteq A\}.$$

Definition 2.13

Let (X, τ_N) be a Neutrosophic topological space. Then A is called

- (i) Neutrosophic regular Closed set [2] (Neu-RCS in short) if $A = \text{Neu-Cl}(\text{Neu-Int}(A))$,
- (ii) Neutrosophic α -Closed set[2] (Neu- α CS in short) if $\text{Neu-Cl}(\text{Neu-Int}(\text{Neu-Cl}(A))) \subseteq A$,
- (iii) Neutrosophic semi Closed set [9] (Neu-SCS in short) if $\text{Neu-Int}(\text{Neu-Cl}(A)) \subseteq A$,
- (iv) Neutrosophic pre Closed set [12] (Neu-PCS in short) if $\text{Neu-Cl}(\text{Neu-Int}(A)) \subseteq A$,

Definition 2.14

Let (X, τ_N) be a Neutrosophic topological space. Then A is called

- (i). Neutrosophic regular open set [2](Neu-ROS in short) if $A = \text{Neu-Int}(\text{Neu-Cl}(A))$,
- (ii). Neutrosophic α -open set [2](Neu- α OS in short) if $A \subseteq \text{Neu-Int}(\text{Neu-Cl}(\text{Neu-Int}(A)))$,
- (iii). Neutrosophic semi open set [9](Neu-SOS in short) if $A \subseteq \text{Neu-Cl}(\text{Neu-Int}(A))$,
- (iv). Neutrosophic pre open set [13] (Neu-POS in short) if $A \subseteq \text{Neu-Int}(\text{Neu-Cl}(A))$,

Definition 2.15

Let (X, τ_N) be a Neutrosophic topological space. Then A is called

- (i). Neutrosophic generalized closed set [4](Neu-GCS in short) if $\text{Neu-cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is a Neu-OS in X ,
- (ii). Neutrosophic generalized semi closed set [12] (Neu-GSCS in short) if $\text{Neu-scl}(A) \subseteq U$ Whenever $A \subseteq U$ and U is a Neu-OS in X ,
- (iii). Neutrosophic α generalized closed set [8](Neu- α GCS in short) if $\text{Neu-}\alpha\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is a Neu-OS in X ,
- (iv). Neutrosophic generalized alpha closed set [8] (Neu-G α CS in short) if $\text{Neu-}\alpha\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is a Neu- α OS in X .

The complements of the above mentioned Neutrosophic closed sets are called their respective Neutrosophic open sets.

Definition 2.18:[5]

Let f be a mapping from an NSTS (X, NS_τ) into NSTS Y, σ . Then f is said to be Neutrosophic generalized continuous (NSG cts) if, $f^{-1}(B) \in \text{NSGCS}(X)$ for every NSCS, B in Y.

Definition 2.18:[5]

Let f be a mapping from an NSTS (X, NS_τ) into NSTS (Y, NS_σ) . Then f is said to be Neutrosophic continuous (NS cts) if, $f^{-1}(B) \in \text{NSOS}(X)$ for every $B \in \sigma$.

Definition 2.19:[12]

A mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ is called Neutrosophic generalized semi continuous (NSGS cts) if, $f^{-1}(B)$ is an NSGSCS in (X, NS_τ) for every NSCS, B of (Y, NS_σ) .

Definition 2.20:

A mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ is called Neutrosophic α generalized continuous (NS α GS cts) if, $f^{-1}(B)$ is an NS α GCS in (X, NS_τ) for every NSCS, B of (Y, NS_σ) .

Definition 2.17:

Let f be a mapping from an NSTS (X, NS_τ) into NSTS (Y, NS_σ) . Then f is said to be

- i) Neutrosophic semi continuous [15] (NS(S) cts) if, $f^{-1}(B) \in \text{NS(S)O}(X)$ for every $B \in \sigma$,
- ii) Neutrosophic α continuous [15] (NS(α) cts) if, $f^{-1}(B) \in \text{NS}(\alpha)\text{O}(X)$ for every $B \in \sigma$,
- iii) Neutrosophic pre continuous [15] (NS(P) cts) if, $f^{-1}(B) \in \text{NS(P)O}(X)$ for every $B \in \sigma$,
- iv) Neutrosophic regular continuous [15] (NS(R) cts) if, $f^{-1}(B) \in \text{NSRO}(X)$ for every $B \in \sigma$.

3. NEUTROSOPHIC WEAKLY π GENERALIZED CONTINUOUS MAPPINGS

In this section, Neutrosophic weakly π generalized continuous mappings is defined. Some of its properties are derived.

Definition 3.1:

A mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ is called an Neutrosophic weakly π generalized continuous mapping (NS(W π G) cts) if, $f^{-1}(B)$ is a NS(W π G)CS in (X, NS_τ) for every NSCS, B of (Y, NS_σ) .

Example 3.2:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{2}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{2}{10}, \frac{5}{10}, \frac{7}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{6}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{7}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle. \text{ Then}$$

$NS_\tau = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_\sigma = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a) = u$ and $f(b) = v$.

Then f is a NS(W π G)CTS mapping.

Proposition 3.3:

Every NSCTS mapping is a NS(W π G)CTS mapping but not conversely.

Proof:

Let $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ be a NSCTS mapping. Let B be a NSCS in Y. Since f is NSCTS mapping, $f^{-1}(B)$ is a NSCS in X. Since every NSCS is a NS(W π G)CS, $f^{-1}(B)$ is a NS(W π G)CS in X. Therefore f is a NS(W π G)CTS mapping.

Example 3.4:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{1}{10}, \frac{5}{10}, \frac{8}{10}\right), \left(\frac{2}{10}, \frac{5}{10}, \frac{7}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{8}{10}, \frac{5}{10}, \frac{1}{10}\right), \left(\frac{7}{10}, \frac{5}{10}, \frac{3}{10}\right) \rangle. \text{ Then}$$

$NS_\tau = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_\sigma = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a)=u$ and $f(b)=v$.

The NSS, $B = \langle y, \left(\frac{1}{10}, \frac{5}{10}, \frac{8}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{7}{10}\right) \rangle$ is NSCS in Y. Then $f^{-1}(B)$ is $NS(W\pi G)CS$ in X, but not NSCS in X. Therefore f is a $NS(W\pi G)CTS$ mapping but not a NSCTS mapping.

Proposition 3.5:

Every $NS(\alpha)$ continuous mapping is a $NS(W\pi G)CTS$ mapping but not conversely.

Proof:

Let $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ be a $NS(\alpha)$ continuous mapping. Let B be a NSCS in Y. Then by definition $f^{-1}(B)$ is a $NS(\alpha)CS$ in X. Since every $NS(\alpha)CS$ is a $NS(W\pi G)CS$, $f^{-1}(B)$ is a $NS(W\pi G)CS$ in X. Thus f is a $NS(W\pi G)CTS$ mapping.

Example 3.6:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{5}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{2}{10}, \frac{5}{10}, \frac{5}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{4}{10}\right) \rangle.$$

Then $NS_\tau = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_\sigma = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a)=u$ and $f(b)=v$.

The NSS, $B = \langle y, \left(\frac{5}{10}, \frac{5}{10}, \frac{2}{10}\right), \left(\frac{4}{10}, \frac{5}{10}, \frac{3}{10}\right) \rangle$ is NSCS in Y. Then $f^{-1}(B)$ is $NS(W\pi G)CS$ in X, but not $NS(\alpha)CS$ in X. Then f is a $NS(W\pi G)CTS$ mapping but not a $NS(\alpha)$ continuous mapping.

Proposition 3.7:

Every $NS(R)$ CTS mapping is a $NS(W\pi G)CTS$ mapping but not conversely.

Proof:

Let $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ be a $NS(R)CTS$ mapping. Let B be a NSCS in Y. Then by definition $f^{-1}(B)$ is a $NS(R)CS$ in X. Since every $NS(R)CS$ is a $NS(W\pi G)CS$, $f^{-1}(B)$ is a $NS(W\pi G)CS$ in X. So, f is a $NS(W\pi G)CTS$ mapping.

Example 3.8:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{5}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{4}{10}, \frac{5}{10}, \frac{5}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{5}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{5}{10}, \frac{5}{10}, \frac{3}{10}\right) \rangle. \text{ Then}$$

$NS_\tau = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_\sigma = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a)=u$ and $f(b)=v$.

The NSS, $B = \langle y, \left(\frac{4}{10}, \frac{5}{10}, \frac{5}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{5}{10}\right) \rangle$ is NSCS in Y. Then $f^{-1}(B)$ is $NS(W\pi G)CS$ in X, but not $NS(R)CS$ in X. Therefore f is $NS(W\pi G)CTS$ mapping but not a $NS(R)$ CTS mapping.

Proposition 3.9:

Every $NS(P)CTS$ mapping is a $NS(W\pi G)CTS$ mapping but not conversely.

Proof:

Let $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ be a $NS(P)CTS$ mapping. Let B be a NSCS in Y. Then $f^{-1}(B)$ is a $NS(P)CS$ in X. Since every $NS(P)CS$ is a $NS(W\pi G)CS$, $f^{-1}(B)$ is a $NS(W\pi G)CS$ in X. Therefore f is a $NS(W\pi G)CTS$ mapping.

Example 3.10:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{7}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{6}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{4}{10}, \frac{5}{10}, \frac{4}{10}\right) \rangle.$$

Then $NS_\tau = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_\sigma = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a)=u$ and $f(b)=v$.

The NSS, $B = \langle y, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{4}{10}, \frac{5}{10}, \frac{4}{10}\right) \rangle$ is NSCS in Y. Then $f^{-1}(B)$ is $NS(W\pi G)CS$ in X, but not $NS(P)CS$ in X. Therefore f is $NS(W\pi G)CTS$ mapping but not a $NS(P)CTS$ mapping.

Proposition 3.11:

Every NS(G)CTS mapping is a NS(WπG)CTS mapping but not conversely.

Proof:

Let $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ be a NS(G)CTS mapping. Let B be a NSCS in Y. Since f is a NS(G)CTS mapping, $f^{-1}(B)$ is a NS(G)CS in X. Since every NS(G)CS is a NS(WπG)CS, $f^{-1}(B)$ is a NS(WπG)CS in X. Thus f is a NS(WπG)CTS mapping.

Example 3.12: Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{2}{10}, \frac{5}{10}, \frac{7}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{6}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{8}{10}, \frac{5}{10}, \frac{2}{10}\right), \left(\frac{7}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle.$$

Then $NS_{\tau} = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_{\sigma} = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ by $f(a)=u$ and $f(b)=v$.

The NSS, $B = \langle y, \left(\frac{2}{10}, \frac{5}{10}, \frac{8}{10}\right), \left(\frac{2}{10}, \frac{5}{10}, \frac{7}{10}\right) \rangle$ is NSCS in Y, $f^{-1}(B)$ is NS(WπG)CS in X but not NS(G)CS in X.

Therefore f is NS(WπG)CTS mapping but not a NS(G)CTS mapping.

Proposition 3.13:

Every NS(αG) continuous mapping is a NS(WπG)CTS mapping but not conversely.

Proof:

Let $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ be a NS(αG) continuous mapping. Let B be a NSCS in Y. Then by definition, $f^{-1}(B)$ is a NS(αG)CS in X. Since every NS(αG)CS is a NS(WπG)CS, $f^{-1}(B)$ is a NS(WπG)CS in X. So, f is a NS(WπG)CTS mapping.

Example 3.14:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{4}{10}, \frac{5}{10}, \frac{2}{10}\right), \left(\frac{6}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle,$$

$G_2 = \langle y, \left(\frac{6}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{2}{10}, \frac{5}{10}, \frac{3}{10}\right) \rangle$. Then $NS_{\tau} = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_{\sigma} = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ by $f(a)=u$ and $f(b)=v$.

The NSS, $B = \langle y, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle$ is NSCS in Y. Then $f^{-1}(B)$ is NS(WπG)CS in X, but not NS(αG)CS in X. Therefore f is NS(WπG) CTS mapping but not a NS(αG) continuous mapping.

Remark 3.15:

NSS continuous mapping and NS(WπG)CTS mapping are independent to each other.

Example 3.8: Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{7}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{6}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{7}{10}, \frac{5}{10}, \frac{3}{10}\right) \rangle.$$

Then $NS_{\tau} = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_{\sigma} = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ by $f(a)=u$ and $f(b)=v$.

Then f is NSS continuous mapping but not a NS(WπG)CTS mapping,

since $B = \langle y, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle$ is a NSSCS in Y,

but $f^{-1}(B) = \langle x, \left(\frac{4}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle$ is not a NS(WπG)CS in X.

Example 3.16:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{9}{10}, \frac{5}{10}, \frac{1}{10}\right), \left(\frac{7}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{3}{10}, \frac{5}{10}, \frac{4}{10}\right), \left(\frac{7}{10}, \frac{5}{10}, \frac{6}{10}\right) \rangle.$$

Then $NS_{\tau} = \{0_{NS}, G_1, 1_{NS}\}$ and $NS_{\sigma} = \{0_{NS}, G_2, 1_{NS}\}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ by $f(a)=u$ and $f(b)=v$. Then f is NS(WπG)CTS mapping, but not a NSS

continuous mapping, since $B = \langle y, \left(\frac{7}{10}, \frac{5}{10}, \frac{3}{10}\right), \left(\frac{6}{10}, \frac{5}{10}, \frac{4}{10}\right) \rangle$ is a NS(WπG)CS in Y,

but $f^{-1}(B) = \langle x, \left(\frac{7}{10}, \frac{5}{10}, \frac{3}{10}\right), \left(\frac{6}{10}, \frac{5}{10}, \frac{4}{10}\right) \rangle$ is not a NSSCS in X.

Remark 3.17: NS(GS) CTS mapping and NS(WπG)CTS mapping are independent to each other.

Example 3.18: Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{2}{10}, \frac{5}{10}, \frac{5}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{5}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{5}{10}, \frac{5}{10}, \frac{2}{10}\right), \left(\frac{5}{10}, \frac{5}{10}, \frac{3}{10}\right) \rangle. \text{ Then}$$

$NS_\tau = \{ 0_{NS}, G_1, 1_{NS} \}$ and $NS_\sigma = \{ 0_{NS}, G_2, 1_{NS} \}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a)=u$ and $f(b)=v$.

Then f is NS(GS) CTS mapping, but not a NS(WπG)CTS mapping,

since $B = \langle y, \left(\frac{2}{10}, \frac{5}{10}, \frac{5}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{5}{10}\right) \rangle$ is a NS(GS)CS in Y,

but $f^{-1}(B) = \langle x, \left(\frac{2}{10}, \frac{5}{10}, \frac{5}{10}\right), \left(\frac{3}{10}, \frac{5}{10}, \frac{5}{10}\right) \rangle$ is not a NS(WπG)CS in X.

Example 3.19:

Let $X = \{a, b\}, Y = \{u, v\}$ and

$$G_1 = \langle x, \left(\frac{5}{10}, \frac{5}{10}, \frac{2}{10}\right), \left(\frac{6}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle,$$

$$G_2 = \langle y, \left(\frac{6}{10}, \frac{5}{10}, \frac{3}{10}\right), \left(\frac{6}{10}, \frac{5}{10}, \frac{2}{10}\right) \rangle.$$

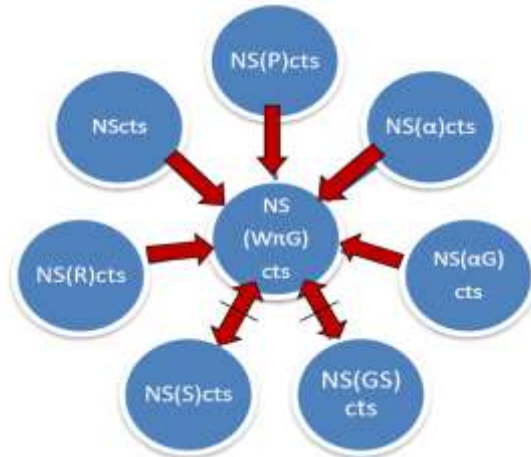
Then $NS_\tau = \{ 0_{NS}, G_1, 1_{NS} \}$ and $NS_\sigma = \{ 0_{NS}, G_2, 1_{NS} \}$ are NSTs on X and Y respectively.

Define a mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ by $f(a)=u$ and $f(b)=v$.

Then f is NS(WπG)CTS mapping, but not a NS(GS) CTS mapping,

since $B = \langle y, \left(\frac{3}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{2}{10}, \frac{5}{10}, \frac{6}{10}\right) \rangle$ is a NS(WπG)CS in Y

but $f^{-1}(B) = \langle x, \left(\frac{3}{10}, \frac{5}{10}, \frac{6}{10}\right), \left(\frac{2}{10}, \frac{5}{10}, \frac{6}{10}\right) \rangle$ is not a NS(GS)CS in X.



4.APPLICATIONS OF NEUTROSOPHIC WEAKLY π GENERALIZED CLOSED MAPPING

Definition 4.1:

An NSTS (X, NS_τ) is called an Neutrosophic wπT1/2 space (NSwπT1/2) if every NSWπGCS in X is an NSCS in X.

Proposition 4.2:

A mapping $f: (X, NS_\tau) \rightarrow (Y, NS_\sigma)$ is NS(WπG) CTS, then the inverse image of each NSOS in Y is a NS(WπG)OS in X.

Proof:

Let B be a NSOS in Y. This implies B^c is NSCS in Y. Since f is NS(WπG) CTS, $f^{-1}(B^c)$ is NS(WπG)CS in X. Since $f^{-1}(B^c) = (f^{-1}(B))^c$, $f^{-1}(B)$ is a NS(WπG)OS in X.

Proposition 4.3:

Let $f: X \rightarrow Y$ be a NS(WπG)CTS mapping and X be a NSwπT1/2 space. Then f is a NSCTS mapping.

Proof:

Let X be a $NS_{\pi}T_{1/2}$ space and B be a NSCS in Y . Then by definition (4.1), $f^{-1}(B)$ is a $NS(W\pi G)CS$ in X . So, $f^{-1}(B)$ is a NSCS in X . Therefore f is a NSCTS mapping.

Proposition 4.4:

A mapping $f: (X, NS_{\tau}) \rightarrow (Y, NS_{\sigma})$ be a $NS(W\pi G)CTS$ mapping and $g \circ f: (Y, NS_{\sigma}) \rightarrow (Z, NS_{\delta})$ is NS continuous, then $g \circ f: (X, NS_{\tau}) \rightarrow (Z, NS_{\delta})$ is a $NS(W\pi G)CTS$.

Proof:

Let D be a NSCS in Z . Then by definition $g^{-1}(D)$ is a NSCS in Y . Since f is a $NS(W\pi G)CTS$ mapping, inverse image of a NSCS in Y is a $NS(W\pi G)CS$ in X . i.e., $f^{-1} \circ g^{-1}(D) = (g \circ f)^{-1}(D)$ is a $NS(W\pi G)CS$ in X . Therefore $g \circ f$ is a $NS(W\pi G)CTS$ mapping.

V. CONCLUSION

Many different forms of closed sets have been introduced over the years. Various interesting problems arise when one considers openness. Its importance is significant in various areas of mathematics and related sciences, In this paper, we introduced the concept of $NS(W\pi G)CTS$ in Neutrosophic Topological Spaces. This shall be extended in the future Research with some applications

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