Novel System and Method for Telephone Network Planning based on Neutrosophic Graph

By Said Broumi, Kifayat Ullah, Assia Bakali, Mohamed Talea, Prem Kumar Singh, Tahir Mahmood, Florentin Smarandache, Ayoub Bahnasse, Santanu Kumar Patro & Angelo de Oliveira

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Abstract - Telephony is gaining momentum in the daily lives of individuals and in the activities of all companies. With the great trend towards telephone networks, whether analogue or digital known as Voice over IP (VoIP), the number of calls an individual can receive becomes considerably high. However, effective management of incoming calls to subscribers becomes a necessity. Recently, much attention has been paid towards applications of single-valued neutrosophic graphs in various research fields. One of the suitable reason is it provides a generalized representation of fuzzy graphs (FGs) for dealing with human nature more effectively when compared to existing models i.e. intuitionistic fuzzy graphs (IFGs), inter-valued fuzzy graphs (IVFGs) and bipolar-valued fuzzy graphs (BPVFGs) etc. In this paper we focused on precise analysis of useful information extracted by calls received, not received due to some reasons using the properties of SVNGs. Hence the proposed method introduced one of the first kind of mathematical model for precise analysis of instantaneous traffic beyond the Erlang unit. To achieve this goal an algorithm is proposed for a neutrosophic mobile network model (NMNM) based on a hypothetical data set. In addition, the drawback and further improvement of proposed method with a mathematical proposition is established for it precise applications.

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I. Introduction

Telephony, appeared in the 1830s, it was based on music notes, for the exchange of messages. It then became a communication system essentially ensuring the transmission and reproduction of speech. Telephony also enables more advanced services such as voicemail, conference calling or voice services. Telephony is based on a telecommunications network, typically, telephone network consists of four main types of equipment: terminals, central systems, ancillary servers, and the access media. We mainly distinguish three types of access media: (i) Land line network, known as Public Switched Telephone Network (PSTN), (ii) wireless network, known as mobile networks, and (iii) private network, whose companies have their own call centre. According to the last report published by the National Telecommunications Regulatory Agency (ANRT) of the kingdom of Morocco, the rate of possession of individuals (12 to 65 years) by mobile phone is slightly increasing in May 2017 (95% against 94.4% in 2015), the use of smartphones by individuals recorded a notable evolution and increased to 67% instead of 54.7% in 2015 [1]. With the rapid explosion on access to the telephone network, the number of calls received becomes considerable. Nowadays, the terms "priority of incoming call", "priority of numbers", "trust of calling equipment", etc. are used [2]. Guarantee a quality of experience (QoE) for the customer is therefore becoming a necessity and especially a promoter axis. However, the amount of information that the service provider must process to ensure QoE is very high, and the decision to route, hold, or reject the incoming call must be at real-time.

Recent time the theory of graph is utilized for various process to deal with uncertainty and vagueness in data sets. It is a mathematical tool which deals with large number of data or information in efficient manner. Graph theory is one of the richest research area in mathematics as it has applications in enormous fields including management sciences [3], social sciences [4], computer sciences [5], communication networks [6], in description of group structures [7], database theory [8], economics [9] etc.

L. A. Zadeh [10] introduced the theory of fuzzy sets (FSs) in 1965 as a tool to deal with uncertainties. It was Kaufmann [11] who define FG but an illustrated work on FGs was done by Rosenfeld in [12]. The theory of FGs is of great importance and in the recent decades, it has been used extensively in many areas such as cluster analysis [13-16], slicing [16], in the solution of fuzzy intersecting equations [17, 18], data base theory [8], networking [19], group structures...
[20, 21], chemical structures [22], navigations [23], traffic controlling [24] etc. The concept of FGs have worth in graph theory as it is the best tool to deal with uncertainties. K. Atanassov [25, 26] proposed the concept of intuitionistic fuzzy sets, an extension of FSs which creates space for IFGs. The concept of IFGs were proposed by R. Parvathi and M. G. Karunambigai [27]. The structure of IFGs is successfully applied in social networks [28], clustering [29], radio coverage network [30] and shortest path problems [31] etc. IFGs effectively deals with uncertainties due to its advance structure. In 1995 F. Smarandache proposed neuinfo logic which provides a base for neutrosophic set (NS) theory [32, 50]. NS theory is a neutrosophic logic which provides a base for generalization of IFSs and among one of the best neutrosophic set based mobilephone network by neutrosophic logic which provides a base for generalization of IFSs and among one of the best

neutrosophic set (NS) theory [32, 50]. NS theory is a neutrosophic logic which provides a base for generalization of IFSs and among one of the best problems the current paper aimed at developing a proposed model and some concluding remark and discussion. article ended with some advantages of proposed model

II. Basic Concepts

In this section, some elementary concepts are demonstrated related to graphs including FGs, IFGs and SVNGs. For undefined terms and notions, one may refer to [34-46, 50].

Definition 1[50]. Neutrosophic Set (NS)

Let \( X \) be a space of points and let \( x \) be a neutrosophic set \( \bar{S} \) in \( X \) is characterized by a truth membership function \( T_\bar{x}(x) \), an indeterminacy membership function \( I_\bar{x}(x) \), and a falsehood membership function \( F_\bar{x}(x) \). The neutrosophic set can be represented as

\[
\bar{S} = \{(x, T_\bar{x}(x), I_\bar{x}(x), F_\bar{x}(x)) : x \in X\}
\]

The sum of \( T_\bar{x}(x) \), \( I_\bar{x}(x) \) and \( F_\bar{x}(x) \) is

\[
0^- \leq T_\bar{x}(x) + I_\bar{x}(x) + F_\bar{x}(x) \leq 3^+
\]

To use neutrosophic set in the real life applications such as engineering and scientific problems, it is necessary to consider the interval \([0, 1]\) instead of \([0^-, 3^+]\) for technical applications.

Definition 2: A pair \( G = (V, E) \) is known as

1. Fuzzy graph if
   a) \( V = \{v_i : i \in I\} \) and \( T_1 : V \rightarrow [0, 1] \) is the association degree of \( v_i \in V \).
   b) \( E = \{(v_i, v_j) : (v_i, v_j) \in V \times V \} \) and \( T_2 : V \times V \rightarrow [0, 1] \) is defined as \( T_2(v_i, v_j) \leq \min[T_1(v_i), T_1(v_j)] \) for all \( (v_i, v_j) \in E \).

2. Intuitionistic fuzzy graph if
   a) \( V = \{v_i : i \in I\} \) such as \( T_1 : V \rightarrow [0, 1] \) is the association degree and \( F_1 : V \rightarrow [0, 1] \) is the disassociation degree of \( v_i \in V \) subject to condition \( 0 \leq T_1 + F_1 \leq 1 \).
   b) \( E = \{(v_i, v_j) : (v_i, v_j) \in V \times V \} \) and \( T_2 : V \times V \rightarrow [0, 1] \) is the association degree and \( F_2 : V \times V \rightarrow [0, 1] \) is the disassociation degree of \( (v_i, v_j) \in E \) defined as \( T_2(v_i, v_j) \leq \min[T_1(v_i), T_1(v_j)] \) and \( F_2(v_i, v_j) \leq \max[F_1(v_i), F_1(v_j)] \) subject to condition \( 0 \leq T_2 + F_2 \leq 1 \) for all \( (v_i, v_j) \in E \).

3. Single-valued neutrosophic graph if
   a) \( V = \{v_i : i \in I\} \) such as \( T_1 : V \rightarrow [0, 1] \) is the association degree, \( I_1 : V \rightarrow [0, 1] \) is the indeterminacy degree and \( F_1 : V \rightarrow [0, 1] \) is the disassociation degree of \( v_i \in V \) subject to condition \( 0 \leq T_1 + I_1 + F_1 \leq 3 \).
III. A Neutrosophic Mobile Network Model

Computing the load of a given Telephone network is one of the major issues for the researchers to extract some useful information for descriptive analysis of carried or offered traffic. It is used to measure by “Erlang Unit” which represents the average number of concurrent calls carried by the given telephone network. As for example a radio channel is busy at all time can be considered as load of 1 Erlang. Similarly, an office having two telephone operators and both are busy on each time. It means the office is having two Erlangs. It means the Erlang unit represents the offered traffic value followed by average number of concurrent calls which is basically depends on call arrival rate, $\lambda$, and the average call-holding time (the average time of a phone call), $h$, given by: (https://en.wikipedia.org/wiki/Erlang_(unit)).

$$E = \lambda h$$  \hspace{1cm} (1)

Where $h$ and $\lambda$ are represented by the same units of time (seconds and calls per second, or minutes and calls per minute).

The problem arises when the user or expert want to analyze the instantaneous traffic to find the exact number of calls received, not received or uncertain due to some reasons to know the level of traffic, recording devices, or solving other security issues. In this case, characterizing the uncertainty and vagueness in telephone network based on its acceptation, rejection and indeterminacy is major problem. To solve this problem current paper introduces a mathematical representation of telephone network using SVNGs where $(T, I, F)$ can further be divided into some situations as given below:

$T$ can be considered as received calls and is divided into subcases $[T_1, T_2, ... T_n]$ where $T_1$ represents...
calls coming from a saved number and $T_2$ represents calls made from some unknown numbers or these can be calls from family member or from friend’s circle or from unknown number etc.

$I$ can be considered as calls which couldn’t be answered due to many reasons $[I_1, I_2, I_3, \ldots I_n]$ represents calls not attended due to driving, busy schedule or meeting or incoming call is from unknown number or any other reason.

$F$ represents those calls which are rejected due to numerous reasons such as $[F_1, F_2, F_3, \ldots F_n]$ stand for rejected calls as incoming call is from unknown number or due to hate or behavior of caller etc.

It is clear from the above explanation that in NMNM, all possibilities can be described effectively. Such a model based on SVNGs described uncertain situation better than crisp graphs or fuzzy graphs or intuitionistic fuzzy graphs due to diverse nature of the NS theory. Moreover, it should be noted that in this network the total number of incoming calls is equal to $T + I + F$ denoted by $S$.

Neutrosophic mobile network model is presented in the following figure 3.

The value of **Truth, neutral and falsity** membership grades can be calculated as

$$w = (T_2, I_2, F_2) = (1, 1, 1)$$

where $S$ is the total number of incoming calls.

The following example illustrate NMNM in a better way.

**Example 1:** Let us suppose 100 calls came on a mobile at end of the day and described in form of following information:

1. 60 calls were received truly among them 50 numbers are saved and 10 were unsaved in mobile. In this case these 60 calls will be considered as truth membership i.e. 0.6.
2. 30 calls were not-received by mobile holder. Among them 20 calls which are saved in mobile contacts were not received due to driving, meeting or phone left in home, car or bag and 10 were not received due to uncertain numbers. In this case all 30 not received numbers by any cause (i.e. driving, meeting or phone left in home) will be considered as Indeterminacy membership i.e. 0.3.

3. 10 calls were those number which was rejected calls intentionally by mobile holder due to behavior of those saved numbers, not useful calls, marketing numbers or other cases for that he/she do not want to pick or may be blocked numbers. In all cases these calls can be considered as false i.e. 0.1 membership value.
The above situation can be represented as:
- neutrosophic set: (0.6, 0.3, 0.1)
- or hesitant neutrosophic set: \((0.5, 0.6), (0.2, 0.3), (0.1, 0.1)\)
- or interval valued neutrosophic set: \([0.5, 0.6], [0.2, 0.3], [0.1, 0.1]\)

**IV. Algorithm**

In this section, an algorithm is proposed describing the flow of NMNM. Here a network of some neutrosophic mobile phones is assumed and the quantity of received, not attended and rejected calls is expressed in the form of single-valued neutrosophic numbers. The NMNM is not limited to store the data of small networks but it can be applied to large networks as well.

- Let \(v_j = (1, 1, 1)\) and \(v_k = (1, 1, 1)\) be two vertices representing two mobile phone numbers.
- Let \(e_{jk} = (T_{jk}, I_{jk}, F_{jk})\) be the edge of \(v_j\) and \(v_k\).
- Let \(S\) denote the number of all calls between two neutrosophic mobile numbers.

\[
\begin{align*}
T_{jk} &= \frac{\text{number of calls received}}{S} \\
I_{jk} &= \frac{\text{number of calls if unattended}}{S} \\
F_{jk} &= \frac{\text{number of calls rejected}}{S}
\end{align*}
\]

This can be written as following propositions:

Let us suppose, total number of all calls between two neutrosophic mobile number = \(s\), \(m\) = total number of calls received, \(n\)-total number of calls rejected then the number of unattended calls are \((s-m-n)\). This can be written as \((s, m-s, s)\) neutrosophic number for determining the \(n^{th}\) call.

Initially one call is made and received then truth value is \(\frac{1}{2} = 1\), indeterminacy value is 0, falsity value is 0. In case two calls are made and received then too truth value is \(\frac{3}{2} = 1\) and so on...

If two calls are made and 1 is received and 1 ignored, then truth is \(\frac{1}{2} = 0.5\) and indeterminacy is \(\frac{1}{2} = 0.5\) so we may say that 50% calls are received and 50% are ignored. If 3 calls are made and number of received, ignored and rejected calls are 1 so we have \((0.33, 0.33, 0.33)\) which make sense that 33% calls are received, 33% calls are ignored and 33% calls are rejected. Similarly, the algorithm works for \(n^{th}\) calls.

The algorithm proposed here explain every possibility that might be happen in a mobile network proving the worth of SVNGs as the most suitable tool for modeling such type of network.

**V. Flowchart**

A flowchart below described the NMNM step by step. It is assumed here that the total number of call could possibly be received or ignored or rejected is 100 (For the sack of simplicity). Here it is also assumed that initially the number of phone calls made so far is zero. In other words, it may be assumed that initially there is no edge between two nodes \(v_j\) and \(v_k\). The illustrated flowchart is described as follows:
In this flow chart, we keep the number of calls limited to 100 but in large networks or in real-life this number of calls cannot be restricted to 100. So, one may set the desired range of calls by their own consent.

**VI. ILLUSTRATED EXAMPLE**

Consider a network of three people connect to each other via mobile phones which are represented by vertices of SVNGs. The following table 1 describe the calling data (total number of calls, received calls, calls not attended and rejected calls) of these three peoples.

**Table 1:** Specifying the calling data of a group

<table>
<thead>
<tr>
<th>Pair</th>
<th>Total calls</th>
<th>Received calls</th>
<th>Not attended calls</th>
<th>Rejected calls</th>
<th>Corresponding Edge</th>
</tr>
</thead>
<tbody>
<tr>
<td>John-Aslam</td>
<td>24</td>
<td>15</td>
<td>5</td>
<td>4</td>
<td>(0.625, 0.208333, 0.166667)</td>
</tr>
<tr>
<td>Aslam-Chris</td>
<td>15</td>
<td>7</td>
<td>5</td>
<td>3</td>
<td>(0.466667, 0.3333, 0.2)</td>
</tr>
<tr>
<td>Chris-Aslam</td>
<td>19</td>
<td>15</td>
<td>4</td>
<td>0</td>
<td>(0.789474, 0.210526, 0)</td>
</tr>
<tr>
<td>Chris-John</td>
<td>5</td>
<td>0</td>
<td>5</td>
<td>0</td>
<td>(0, 1, 0)</td>
</tr>
<tr>
<td>John-Chris</td>
<td>8</td>
<td>4</td>
<td>3</td>
<td>1</td>
<td>(0.5, 0.375, 0.125)</td>
</tr>
</tbody>
</table>
In this example, a network of finite number of people is illustrated. The edges in this network is in the form single-valued neutrosophic numbers showing the percentage of number of calls received, left unattended or rejected. The Figure 5 shows that maximum true calls happens among Chris and Aslam due to maximal true membership-values, minimum indeterminacy and minimum falsity membership-values when compared to others. Similarly, other information can be extracted from the proposed method.

VII. Some Special Circumstances and Significance of Neutrosophic Mobile Network Model

In this part of the article, some special cases are listed to extract meaningful information from the proposed method. It is discussed how proposed model is capable of dealing with such kind of situations. This is done in the following way:

**Question 1:** Is there any difference between saved and unsaved numbers? Did it influence the membership?

**Answer:** The answer to this question should be of the following form:

When both saved and unsaved numbers are

- **Received:** Then truth valued is increased by an amount.
- **Left Unattended:** Then indeterminacy values in increased by an amount.
- **Rejected:** Then falsity value is increased by an amount.

So saved and unsaved numbers are treated equally in such scenario. But In case the number is saved most probably the holder knows the person and pick the phone or reject it most of time. However, when number is unsaved then many times holders do not want to pick which affects indeterminacy membership-values a lot.

**Question 2:** How the proposed model deals with marketing numbers as they are important some time while some other time they are meaningless.

**Answer:** We have introduced a unique scenario to understand the telephone network using single-valued neutrosophic set and its properties as a first basic algorithm when none of the approaches are exists in this regard. Of course, we can control this issue by two cases. The first way is when we do not know that the incoming call is marketing call so it may be rejected or ignored. In second case, when we want to pick the same marketing call in some other time then the number can be saved in the phone as useful number. In this case the first time its membership-values will affect the indeterminacy or falsity value whereas in second case it affects the truth membership-values.

**Question 3:** When a person is in coma, then all calls on his/her mobile shall be left unattended similarly when a person is kidnapped, then all calls on his/her mobile gets rejection. How the proposed method explains such situation?

**Answer:** This is an impressive question towards one of the useful applications of our motive to introduce neutrosophic set in telephone network.

We will first try to understand the first case that is Coma means holder is in the operating system. In this case the call may go but holder cannot pick it due to uncertainty. Hence all the incoming call on holder’s mobile will be unreceived (not rejected only unreceived) which can be clearly shown by \((0, 1, 0)\). For example, suppose 10 calls came on to his/her mobile and are left unattended…. i.e. \(s = 10, m = 0, n = 0\). Then \((\frac{m}{s}, \frac{s-m-n}{s}, \frac{n}{s}) = (0, \frac{10-0-0}{10}, 0) = (0, 1, 0)\)

Now we can understand the case of kidnapping. In this case, the call can be rejected by kidnapper or switch off the phone. It is well known that the kidnapper will not pick the phone or allow to ring the...
bell several times to understand the location. Hence all calls will be rejected and can be represented as \((0, 0, 1)\) for all time. For example, if 10 calls made and rejected. Then \(n = 10, s = 10. (0, \frac{10}{10}, \frac{10-0-10}{10}, \frac{10}{10}) = (0, 0, 1)\).

Hence the proposed NMNM can deal with every possibility than one my face. It shows its significance in extracting some meaningful information from mobile network based on their calls received and rejected. The analysis derived from the proposed method will be helpful in making an intelligent system.

In this article, the mobile network is discussed in the environment of SVNGs. It is observed that such a network cannot be established by ordinary FSs i.e. by FGs as FS theory only deals with association degree. Similarly, such a network is difficult to establish in the environment of IFS theory as it describes the association and dissociation degree of elements but in mobile network models we face several types of situations as described earlier. Therefore, the space of SVNG is so far, a best tool for describing such type of situation and for establishing a mobile network model.

VIII. Conclusion and Discussion

In this article, a method for information analysis in mobile network model is described using SVNGs, known as NMNM for precise representation of instantaneous traffic in an alternative way when compared to Erlang Number. The proposed method also describes the structure of FSs and IFSs to make it less resourceful in establishing such type of network for extracting some useful information. A mathematical proposition is also derived for restructuring the SVNGs to represent the received, un-received as well as uncertain calls when compared for depth analysis. The proposed NMNM model is explained using an illustrative example for better understanding. However, the analysis derived from the proposed method is not implemented in any real data sets. To solve this problem in near future the author will focus on comparative study of the proposed method.

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References Références Referencias


51. Singh P.K., “Interval-valued neutrosophic graph representation of concept lattice and its (α, β, γ)-