

ON THE INTERSECTED SMARANDACHE PRODUCT SEQUENCES

Maohua Le

Zhanjiang Normal College, Zhanjiang, Guangdong, P.R.China

Abstract. In this paper we discuss a question concerning the intersected Smarandache product sequences.

Let $U = \{u_n\}_{n=1}^{\infty}$ be an infinite increasing sequence of positive integers. For any positive integer n , let

$$(1) \quad s_n = 1 + u_1 u_2 \dots u_n .$$

Then the the sequence $S(U) = \{s_n\}_{n=1}^{\infty}$ is called the Smarandache product sequence of U (see[1]). Further, if there exist infinitely many terms in U belonging to $S(U)$, then $S(U)$, is called intersected. In this paper we pose the following question:

Question. Wich of ordinary Smarandache product sequences are intersected?

We nou give some obvious examples as follows:

Example 1. If $U = \{n\}_{n=1}^{\infty}$, then $S(U)$ is intersected. In this case, we see from (1) that $s_n = u_{n-1}$ for any positive integer n .

Exemple 2. Let k be a positive integer with $k > 1$. If $U = \{kn\}_{n=1}^{\infty}$, then $S(U)$ is non-intersected, since $k \nmid s_n$ for any positive integer n .

Exemple 3. Let k be a positive integer with $k > 1$. If $U = \{n^k\}_{n=1}^{\infty}$, then $S(U)$ is non-intersected. In this case, we have $s_n = 1 + 1^k 2^k \dots n^k = 1 + (n!)^k$, which is not a k -th power.

Example 4. If $U = \{n!\}_{n=1}^{\infty}$, then $S(U)$ is non-intersected. In this case, we have $s_n = 1 + 1!2! \dots n!$, which is an odd integer if $n > 1$. It implies that $u_n \in S(U)$ if and only if $n=2$.

Reference

- 1.F.Iacobescu, Smarandache partition type and other sequences, Bull.Pure appl.Sci.Sect.E 16(1997), No.2, 237-240.