## THE PRIMES IN THE SMARANDACHE SYMMETRIC SEQUENCE

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Abstract. Let  $S=\{s_n\}_{n=1}^{n}$  Be the Smarandache symmetric sequence. In this paper we prove that if n is an even integer and  $n/2 \neq 1 \pmod{3}$ , then  $s_n$  is not a prime.

Let  $S=\{s_n\}_{n=1}^{n}$  be the Smarandache symmetric sequence, where

(1)  $s_1=1, s_2=11, s_3=121, s_4=1221, s_5=12321, s_6=123321, s_7=1234321, s_8=12344321, \dots$ 

Smarandache asked how many primes are there among S? (See [1, Notions 3]). In this paper we prove the following result:

Theorem. If n is an iven integer and  $n/2 \neq 1 \pmod{3}$ , then s<sub>n</sub> is not a prime.

Proof. If n is an even integer, then n=2k, where k is a positive integer. We see from (1) that

(2)  $s_n = \overline{12 \dots kk \dots 21}$ 

It implies that

(3) 
$$s_n = 1^* 10^+ 2^* 10^+ \dots + k^* 10^+ k^* 10^+ \dots + 2^* 10^+ 11^* 10^+$$

where  $t_1, t_2, ..., t_{2k}$  are nonnegative integers. Since 10<sup>t</sup> = 1 (mod 3) for any nonnegative integer t, we get from (3) that

(4)  $s_n \equiv 1+2+...+k+k+...+2+1 \equiv k(k+1) \pmod{3}$ . If  $k \neq 1 \pmod{3}$ , then either  $k \equiv 0 \pmod{3}$  or  $k \equiv 2 \pmod{3}$ . In both cases, we have  $k(k+1) \equiv 0 \pmod{3}$  and  $3 \mid s_n$  by (4). Thus,  $s_n$  is not a prime. The theorem is proved.

Reference

1. Dumitrescu and Seleacu, Some Notions and Questions In Number Theory, Erhus Univ. Press, Glendale, 1994.