## THE SQUARES IN THE SMARANDACHE FACTORIAL PRODUCT SEQUENCE OF THE SECOND KIND

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Abstract. In this paper we prove that the Smarandache factorial product sequence contains only one square 1.

Key words . Smarandache product sequence, factorial, square.

For any positive integer n, let

(1) 
$$F(n) = \prod_{k=1}^{n} k! - 1$$
.

Then the sequence  $F = \{F(n)\}_{n=1}^{\infty}$  is called the Smarandache factorial product sequence of the second kind (see [2]). In this paper we completely determine squares in F. We prove the following result.

**Theorem**. The Smarandache factorial product sequence of the second kind contains only one square F(2)=1.

**Proof.** Since F(1)=0 by (1), we may assume that n>1. If F(n) is a square, then from (1) we get

(2) 
$$a^2 = \prod_{k=1}^n k!,$$

where a is a positive integer. By [1,Theorem 82], if p is a prime divisor of  $a^2+1$ , then either p=2 or  $p \equiv 1 \pmod{4}$ . Therefore, we see from (2) that n<3. Since F(2)=1 is a square, the theorem is proved.

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## References

- [1] G.H Hardy and E.M. Wright, An Introduction to the Theory of Numbers, Oxford University Press, Oxford, 1937.
- [2] F. Russo, Some results about four Smarandache Uproduct sequence, Smarandache Notions J. 11(2000)42-49.

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