



# Single Valued Neutrosophic Kruskal-Wallis and Mann Whitney Tests

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**Abstract:** In this paper, Kruskal-Wallis test is extended to deal with neutrosophic data in single valued form using score, accuracy and certainty functions to calculate ranks of SVNNs, also Mann-Whitney test is extended to deal with same data type which makes it possible to do a post-hoc test after rejecting null hypothesis using Neutrosophic Statistics Kruskal-Wallis test. Numerical examples were successfully solved showing the power of this new idea to deal with SVNNs and make statistical decisions on them.

**Keywords:** Kruskal-Wallis; Test Statistic; Chi Square Distribution; Hypothesis Testing; Significance Level; Single Valued Neutrosophic Number.

# 1. Introduction

F. Smarandache presented neutrosophic logic as an extension to fuzzy logic [1] and intuitionistic fuzzy logic [2] to deal with indeterminacy, ambiguity, uncertainty, contradiction, unsureness, nihilness, vagueness and emptiness [3], this new extension make decisions more flexible and reliable [4] [5] and has been applied in many scientific fields including abstract algebra, mathematical modelling, probability theory, statistics, operations research, artificial intelligence, machine learning, etc. [6] [5] [7] [8] [9] [10] [11] [12] [13] [14] [15] [16] [17] [18]. He also introduced the Neutrosophic Statistics as an extension of the Interval Statistics, since the neutroosphic statistics may deal with all types of indeterminacies (with respect to the data, inferential procedures, probability distributions, graphical representations, etc.), it allows the reduction of indeterminacy, and it uses the neutrosophic probability that is more general than imprecise and classical probabilities, and has more detailed corresponding probability density functions - while Interval Statistics only deals with indeterminacy that can be represented by intervals. [27].

In statistics, M. Aslam presented many neutrosophic statistical tests to deal with indeterminacy in data considering that observations are classical neutrosophic numbers of the form N = D + I where *D* is the determinant part of the number and *I* is its indeterminant part [19] [20] [21] [22].

Comparing population means is one of the most important statistical tests to test whether several drawn samples are from one population (then we say that means are equal) or from different populations (here we say that means are not equal). This procedure is done using hypothesis testing with respect to a test statistic having a previously known probability distribution comparing its value with acceptance region and rejection region.

The problem arises when dealing with neutrosophic number or judges, e.g., if a doctor says that a patient is 70% infected with COVID-19 with 20% indeterminacy because of similar flu syndromes and with 50% chance to be wrong diagnosis, here we cannot deal with this data type using classical statistical tests neither with previously studied neutrosophic statistical tests.

A mathematical solve for this problem in lattice theory and abstract algebra was presented in [23] where ranking of observations was done and presented in [24] to compare between judges. also, previous work was generalized in [25] [26].

In this paper we are going to solve this problem from statistical point of view where we are dealing with samples data derived from different populations to make generalize decisions made based on samples to population extending Kruskal-Wallis test to deal with (T, I, F) data sets which is the well-known single valued neutrosophic numbers and make it possible to compare several samples and take decision if those samples are drawn from same population or from different populations, then we will extend Mann-Whitney test to make a multiple comparison between each two groups.

#### 2. Preliminaries

We recall here some basic definitions of single valued neutrosophic sets and single valued neutrosophic numbers and some operations on them.

## 2.1 Single Valued Neutrosophic Sets:

Suppose that  $\Omega$  is the universe and let A be a subset of  $\Omega$  then A is said to be Single Valued Neutrosophic Set (SVNS) with truth, indeterminacy and falsity memberships and denoted as follows:  $A = \{ (x|T_A(x), I_A(x), F_A(x)) \}$ 

Where:

$$\begin{split} T_A &: \Omega \to [0,1] \\ I_A &: \Omega \to [0,1] \\ F_A &: \Omega \to [0,1] \end{split}$$

And:

$$0 \le T_A(x) + I_A(x) + F_A(x) \le 3$$

#### 2.2 Single Valued Neutrosophic Numbers:

Single Valued Neutrosophic Number (SVNN) takes the form (*T*, *I*, *F*) where *T* reflects truth, *I* reflects indeterminacy and *F* reflects falsity where  $0 \le T, I, F \le 1$  and  $0 \le T + I + F \le 3$ .

#### 2.3 Operations on Single Valued Neutrosophic Numbers:

Suppose that  $A = (t_1, i_1, f_1), B = (t_2, i_2, f_2)$  are two SVNNs then operations on A, B are defined as follows:

$$\begin{split} A \bigoplus B &= (t_1 + t_2 - t_1 t_2, i_1 i_2, f_1 f_2) \\ A \bigotimes B &= (t_1 t_2, i_1 + i_2 - i_1 i_2, f_1 + f_2 - f_1 f_2) \\ A \bigoplus B &= \left(\frac{t_1 - t_2}{1 - t_2}, \frac{i_1}{i_2}, \frac{f_1}{f_2}\right); t_2 \neq 1; i_2 \neq 0; f_2 \neq 0 \\ \frac{A}{B} &= \left(\frac{t_1}{t_2}, \frac{i_1 - i_2}{1 - i_2}, \frac{f_1 - f_2}{1 - f_2}\right); t_2 \neq 0; i_2 \neq 1; f_2 \neq 1 \\ \lambda A &= (1 - (1 - t_1)^{\lambda}, i_1^{\lambda}, f_1^{\lambda}); \lambda > 0 \\ A^{\lambda} &= \left(t_1^{\lambda}, 1 - (1 - i_1)^{\lambda}, 1 - (1 - f_1)^{\lambda}\right); \lambda > 0 \end{split}$$

## 2.4 Ranking of Single Valued Neutrosophic Numbers

Let A(T, I, F) be a SVNN, the score function s(A), accuracy function a(A) and certainty function c(A) are defined as follows:

 $s(A) = \frac{2 + T - I - F}{3}$ a(A) = T - Fc(A) = T

We can rank *A*, *B* using the following algorithm:

- 1) If s(A) > s(B) then A > B.
- 2) If s(A) = s(B) and a(A) > a(B) then A > B.
- 3) If s(A) = s(B) and a(A) = a(B) and c(A) > c(B) then A > B.
- 4) If s(A) = s(B) and a(A) = a(B) and c(A) = c(B) then A = B

#### 3. Classical Kruskal-Wallis and Mann Whitney Tests

Kruskal-Wallis Test (H Test) one of the nonparametric tests that based on ranks used to compare the means of c independent random samples of sizes  $n_1, ..., n_c$  drawn from c univariate populations with unknown cumulative distribution functions  $F_1, ..., F_c$ .

The technique of (H Test) performed by ranking all observation and defined as follows:

Formally, letting the distribution function of *X* over the group i be of the form  $F_i(x) = F(y - \theta_i)$ , we'd like to test

$$H_0: \theta_1 = \theta_2 = \dots = \theta_c$$
 against  $H_1: \theta_i \neq \theta_i$  for some  $i, j$ 

The test is based on  $\chi^2(c-1)$  distribution using test statistic:

$$H = \frac{12}{N(N+1)} \sum_{i=1}^{C} \frac{R_i^2}{n_i} - 3(N+1)$$

Where:

c number of samples

 $n_i$  number of observations in the i<sup>th</sup> group

 $N = \sum n_i$  number of observations in all samples

 $R_i$  sum of ranks for the i<sup>th</sup> group

Notice that H test tells us whether the samples are drawn from same population (when accepting  $H_0$ ) or those sample are drawn from different populations.

If we reject  $H_0$  then we must determine the true differences location, i.e. we must do a post hoc test, and one of the famous used tests is Mann Whitney test that tests the following hypothesis:

$$H_0: \theta_i = \theta_j$$
$$H_1: \theta_i \neq \theta_j$$

 $Z = \frac{U - \overline{U}}{std_{II}}$ 

Using test statistic:

Where:

$$\overline{U} = \frac{n_i n_j}{2}$$

$$std_U = \sqrt{\frac{n_i n_j (n_i + n_j + 1)}{12}}$$

$$U = \min\left(n_i n_j + \frac{n_i (n_j + 1)}{2} - R_i, n_i n_j + \frac{n_j (n_j + 1)}{2} - R_j\right)$$

#### 4. Single Valued Neutrosophic Kruskal Wallis and Mann Whitney Tests

Suppose that we have c random samples as follows:

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Sample 1	Sample 2	•••	Sample c
<i>S</i> <sub>11</sub>	S <sub>21</sub>		$S_{c1}$
<i>S</i> <sub>12</sub>	S <sub>22</sub>	•.	$S_{c2}$
:	:		

 Table 1. Neutrosophic Observations.

$$S_{1n_1}$$
  $S_{2n_2}$   $S_{cn_c}$ 

Where  $S_{11}, S_{12}, ..., S_{cn_c}$  are SVNNs, e.g., judgments, sentiments, point of views, considerations, ... etc. and we would like to check whether these judgments are consistent. Kruskal Wallis test can answer our question but the problem that arises is how to calculate the ranks of these judges since it is base on neutrosophic numbers. We will present the following algorithm to solve this problem:

- 1. Merge all the observation from different samples and deal with it as one sample.
- 2. Calculate score, accuracy and certainty of each observation.
- 3. Compare and rank these observations based on its score, accuracy and certainty.
- 4. Give the ranked observations ranks from 1 to *N* and if we have two equal observation the we average its ranks.
- 5. Compute Kruskal Wallis test statistic using the formula:

$$H_N = \frac{12}{N(N+1)} \sum_{i=1}^{5} \frac{(R_i^2)_N}{n_i} - 3(N+1)$$

where  $(R_i^2)_N$  is sum of i<sup>th</sup> sample neutrosophic rank, hence  $H_N$  is neutrosophic test statistic.

- 6. Compare the test statistic with  $\chi_{1-\alpha}^2(c-1)$  critical values, if  $H_N < \chi_{1-\alpha}^2(c-1)$  then samples are drawn from same population, i.e., judgments are consistent and here test is done. elsewhere judgments are inconsistent and we must go to step 7.
- 7. Compute Mann Whitney test statistic pairwise based on ranked data using steps 1-4 using the formula:

$$Z_N = \frac{U_N - \overline{U}_N}{std_{U_N}}$$

Where:

$$\overline{U_N} = \frac{n_i n_j}{2}$$

$$std_{U_N} = \sqrt{\frac{n_i n_j (n_i + n_j + 1)}{12}}$$

$$U_N = \min\left(n_i n_j + \frac{n_i (n_j + 1)}{2} - (R_i)_N, n_i n_j + \frac{n_j (n_j + 1)}{2} - (R_j)_N\right)$$

8. if  $|Z_N| < Z_{1-\frac{\alpha}{2}}$  then two compared samples are drawn from same population and otherwise samples are drawn from different populations.

#### Example 4.1

We would like to compare judgments of 3 independent doctors on infecting with COVID-19 for 10 sick people, each doctor is confident T% and unsure I% and may be giving wrong judgment F%.

Table 2. Neutrosophic judgments of infecting with COVID-19.

			1 )	0	0			
	Α			В			С	
т	I	F	Т	I	F	т	I	F
0.207	0.922	0.550	0.905	0.808	0.657	0.949	0.034	0.000
0.879	0.968	0.419	0.555	0.238	0.571	0.057	0.842	0.398
0.200	0.825	0.208	0.726	0.552	0.689	0.845	0.042	0.662
0.824	0.378	0.011	0.230	0.046	0.825	0.858	0.622	0.833
0.859	0.988	0.654	0.779	0.470	0.897	0.853	0.055	0.383
0.874	0.347	0.499	0.599	0.293	0.607	0.416	0.092	0.972
0.842	0.772	0.402	0.007	0.013	0.371	0.407	0.330	0.140
0.855	0.999	0.378	0.688	0.027	0.571	0.978	0.257	0.495
0.368	0.458	0.078	0.940	0.628	0.441	0.048	0.109	0.983

0.698 0.220 0.712 0.614 0.003 0.628 0.110 0.509 0.063
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First, we calculate score, accuracy and	l certainty of the previous data as follows:
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S(A)	S(B)	S(C)	A(A)	A(B)	A(C)	C(A)	C(B)	C(C)
0.245	0.480	0.972	-0.343	0.248	0.949	0.207	0.905	0.949
0.497	0.582	0.272	0.460	-0.016	-0.341	0.879	0.555	0.057
0.389	0.495	0.714	-0.008	0.037	0.183	0.200	0.726	0.845
0.812	0.453	0.468	0.813	-0.595	0.025	0.824	0.230	0.858
0.406	0.471	0.805	0.205	-0.118	0.470	0.859	0.779	0.853
0.676	0.566	0.451	0.375	-0.008	-0.556	0.874	0.599	0.416
0.556	0.541	0.646	0.440	-0.364	0.267	0.842	0.007	0.407
0.493	0.697	0.742	0.477	0.117	0.483	0.855	0.688	0.978
0.611	0.624	0.319	0.290	0.499	-0.935	0.368	0.940	0.048
0.589	0.661	0.513	-0.014	-0.014	0.047	0.698	0.614	0.110

Table 3. Score, accuracy and certainty of judgments.

Then we rank our neutrosophic numbers based on its score, accuracy and certainty as follows:

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Doctor	Score	Accuracy	Certainty	Rank			
А	0.139	-0.598	0.074	1			
А	0.33	-0.148	0.754	5			
А	0.383	-0.535	0.31	9			
А	0.426	0.003	0.638	14			
А	0.44	-0.047	0.803	15			
А	0.507	0.379	0.733	21			
А	0.56	0.06	0.746	23			
А	0.568	-0.115	0.723	24			
Α	0.665	0.206	0.442	28			
Α	0.822	0.584	0.642	30			
В	0.206	-0.449	0.023	3			
В	0.288	-0.434	0.541	4			
В	0.352	-0.085	0.569	6			
В	0.37	0.03	0.906	8			
В	0.385	-0.658	0.23	11			
В	0.406	0.194	0.342	12			
В	0.424	-0.382	0.545	13			
В	0.559	-0.2	0.614	22			
В	0.594	-0.058	0.343	25			
В	0.624	0.125	0.826	26			
С	0.181	-0.921	0.022	2			
С	0.362	-0.353	0.231	7			
С	0.383	-0.037	0.472	10			
С	0.468	0.363	0.446	16			
С	0.474	-0.217	0.393	17			

Table 4. Ranks of judgments.

С	0.489	-0.158	0.737	18
С	0.499	-0.238	0.755	19
С	0.504	0.017	0.854	20
С	0.66	0.107	0.653	27
С	0.705	0.399	0.709	29

Now we rearrange samples and calculate sum of each sample neutrosophic ranks and we get:

 $(R_A)_N = 170, (R_B)_N = 130, (R_C)_N = 165$ 

And test statistic is:

$$H_N = \frac{12}{30(30+1)} \left( \frac{170^2 + 130^2 + 165^2}{10} \right) - 3(30+1) = 1.2258$$

Comparing with critical value say at 0.05 significance level we find that  $H_N = 1.2258 < \chi^2(2) = 5.9915$  so we accept the null hypothesis and we say that all judgments are consistent.

#### Example 4.2

3 samples of students were drawn to test whether there is a significant difference between nervous before exam where 3 sets of students were following three strategies of learning, data is shown in Table 5:

	Α			В			С	
Т	I	F	Т	I	F	Т	I	F
0.399	0.056	0.457	0.127	0.4545	0.3855	0.152	0.622	0.292
0.4155	0.0705	0.373	0.0025	0.0735	0.083	0.498	0.143	0.748
0.037	0.5	0.206	0.0095	0.171	0.4055	0.357	0.831	0.625
0.4635	0.137	0.3055	0.442	0.2785	0.4225	0.464	0.761	0.551
0.0755	0.029	0.171	0.003	0.4755	0.3055			
0.3335	0.2995	0.207	0.0615	0.072	0.184			

Table 5. Nervous Before Exam.

First, we calculate score, accuracy and certainty of the previous data as follows:

S(A) S(B) S(C) A(A) A(B) A(C) C(A) C(B) C(C) 0.629 0.429 0.413 -0.058 -0.259 -0.140 0.399 0.127 0.152 0.657 0.615 0.536 0.043 -0.081 -0.250 0.416 0.003 0.498 0.444 0.478 0.300 -0.396 -0.268 -0.169 0.037 0.010 0.357 0.674 0.580 0.384 0.158 0.020 -0.087 0.464 0.442 0.464 0.625 0.407 -0.096 -0.303 0.076 0.003 0.609 0.602 0.334 0.127 -0.123 0.062

**Table 6.** Score, accuracy and certainty of nervous.

Then we rank our neutrosophic numbers based on its score, accuracy and certainty as follows:

Learning Strategy	Score	Accuracy	Certainty	Rank
А	0.674	0.158	0.4635	16
А	0.657	0.0425	0.4155	15
А	0.629	-0.058	0.399	14
А	0.625	-0.0955	0.0755	13
А	0.609	0.1265	0.3335	11

Table 7. Ranks of nervous.

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А	0.444	-0.169	0.037	6
В	0.615	-0.0805	0.0025	12
В	0.602	-0.1225	0.0615	10
В	0.580	0.0195	0.442	9
В	0.478	-0.396	0.0095	7
В	0.429	-0.2585	0.127	5
В	0.407	-0.3025	0.003	3
С	0.536	-0.25	0.498	8
С	0.413	-0.14	0.152	4
С	0.384	-0.087	0.464	2
С	0.300	-0.268	0.357	1

Now we rearrange samples and calculate sum of each sample neutrosophic ranks and we get:  $(R_A)_N = 75, (R_B)_N = 46, (R_C)_N = 15$ 

And test statistic is:

$$H_N = \frac{12}{16(16+1)} \left( \frac{75^2}{6} + \frac{46^2}{6} + \frac{15^2}{4} \right) - 3(16+1) = 8.4007$$

Comparing with critical value, say at 0.05 significance level, we find that  $H_N = 8.4007 > \chi^2(2) =$  5.9915 so we reject the null hypothesis and we say that level of nervous are not equal, so we must perform Neutrosophic Mann Whitney Test and we have three cases:

Case 1 between A, B:

$$U_{N} = \min\left(n_{1}n_{2} + \frac{n_{1}(n_{1}+1)}{2} - (R_{A})_{N}, n_{1}n_{2} + \frac{n_{2}(n_{2}+1)}{2} - (R_{B})_{N}\right) = \min(5,31) = 5$$

$$\overline{U_{N}} = \frac{n_{1}n_{2}}{2} = 18$$

$$std_{U_{N}} = \sqrt{\frac{n_{1}n_{2}(n_{1}+n_{2}+1)}{12}} = 6.244998$$

$$Z_{N} = \frac{U_{N} - \overline{U_{N}}}{std_{U_{N}}} = -2.08167$$

So  $|Z_N| > Z_{0.975} = 1.96$  and hence we reject the null hypothesis and take alternative hypothesis and methods A, B making different nervous level, since  $\overline{R_A} = \frac{75}{6} = 12.5 > \overline{R_B} = 7.667$  then nervous level of group A is higher than nervous level of group B.

Case 2 between B, C:

Following same steps, we see that  $|Z_N| = |-1.7056| < 1.96$  so there is no difference in nervous level between group B and C.

Case 3 between A, C:

Following same steps, we see that  $|Z_N| = |-2.3452| > 1.96$  so there is a significant difference in nervous level between group A and C and nervous level of group A is higher than nervous level of group C because  $\overline{R_A} = \frac{75}{6} = 12.5 > \overline{R_C} = \frac{15}{4} = 3.75$ .

## 5. Conclusions

In this paper we have solved the problem of making statistical tests on single valued neutrosophic number-based problems which wasn't solved before. An algorithm to perform Kruskal-Wallis test and Mann Whitney test when dealing with SVNNs is presented and numerical examples were solved successfully in two fields of real-life problems, medical field and educational field. In future we are looking forward to extend other statistical tests which are important in decision making problems.

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